# Convergence Across Castes<sup>\*</sup>

Viktoria Hnatkovska

Chenyu(Sev) Hou

University of British Columbia

Simon Fraser University

Amartya Lahiri University of British Columbia December 2, 2024

#### Abstract

India witnessed a sharp education and wage catch-up by the historically disadvantaged scheduled castes and tribes (SC/STs) towards non-SC/ST levels during the period 1983-2012. We provide a structural explanation for the catch-up using a multi-sector, heterogenous agent model where individuals differ in ability and their caste identity. Castes differ in the costs of schooling and accessing sectoral labor markets which results in caste-based talent misallocations. We show that exogenous productivity growth can explain 72 percent of the observed wage convergence. The primary driver of convergence in the model is the fall in real costs of schooling with growth. We provide independent evidence in support of this mechanism.

JEL Classification: J6, R2

Keywords: Castes, convergence, growth

## 1 Introduction

Caste identities are fundamentally enmeshed in the social, economic and political lives of people in India. These identities, which are determined by birth, often dictate where they grow up, where they study, where they work, who they marry and who they network with. Given the rigid nature

<sup>&</sup>lt;sup>\*</sup>We would like to thank Tasso Adamopoulos, Paul Beaudry, Satyajit Chatterjee, Rana Hasan, Chang-Tai Hsieh, Ashok Kotwal, Devashish Mitra, Dilip Mookherjee, B. Ravikumar, Richard Rogerson, and seminar participants at the CMSG-Montreal, IGC conference (Delhi), FRB St Louis-LAEF-Human Capital conference in Santa Barbara, NBER Summer Institute, IIT-Delhi, IIT-Kanpur, UCSD, Peking University, Pennsylvania State University, FRB Philadelphia, University of Maryland and USC for helpful comments and discussions. Thanks to Sudipta Ghosh for providing research assistance. We also thank the IGC for providing funding to support this research.

of birth-based caste hierarchies, it was often viewed as an immovable barrier to socio-economic mobility.  $^{\rm 1}$ 

After India's independence from British rule in 1947, framers of the constitution of modern India were acutely aware of the need to create a level playing field for all Indians in the newly independent country. To facilitate this, the constitution identified the most disadvantaged castes and tribes and collected them in a schedule of the Indian constitution. This identified group is today referred to as Scheduled Castes and Tribes or SC/STs. The constitution mandated reservations for SC/STs in higher education, public sector jobs and political representation as a way of redressing their historical disadvantage.

Recent work by Hnatkovska et al. (2012) has shown that the period since 1983 has witnessed a sharp reduction in education and wage disparities between non-SC/STs and SC/STs with most of the wage convergence being empirically accounted for by education convergence.<sup>2</sup> These trends represent a remarkable turnaround in the fortunes of SC/STs after centuries of disadvantage.

What sparked this convergence? There are no clear answers to this question even though answers are crucial from a policy standpoint. Munshi (2019) conjectures that affirmative action policies as well as caste-based labor networks may have been contributing factors. While there is scholarly work that examines the effects of networks and reservations in local contexts, there is no evidence on the dynamic effects of either of these caste-specific mechanisms on caste gaps at the aggregate level.<sup>3</sup>

Despite the lack of systematic evidence on their aggregate effects, the demand for more caste based social welfare and economic protections has continued to rise in India. In 2022, the state of Bihar conducted a survey to enumerate the caste distribution at a granular level that went beyond the coarse SC/ST-non-SC/ST binary classification. The goal of this effort is for the state government to better target social welfare schemes to different castes. Many other states in India are also considering conducting similar surveys. The implicit consensus appears to be that inequalities across castes are best addressed by targeted social welfare and affirmative action programs.

There are reasons, however, to believe that factors other than caste-specific policies or mech-

<sup>&</sup>lt;sup>1</sup>Munshi (2019) provides an excellent background and overview of the role of castes in India.

 $<sup>^{2}</sup>$ On a related theme, Hnatkovska et al. (2013) show that the intergenerational mobility rates of SC/STs in terms of education and wages have also caught up to non-SC/ST rates.

<sup>&</sup>lt;sup>3</sup>Munshi and Rosenzweig (2016) shows evidence for the effects of caste networks on migration decisions in India. Their results suggest that caste networks may have slowed down urban migration. On the effects of reservations, Bertrand et al. (2010) examines their impact on enrolment and outcomes in engineering colleges in one Indian state in 1996. However, neither paper nor the mechanisms that they examine map directly into the time series evolution of aggregate caste wage gaps, which is the focus of this paper.

anisms may have been at play in India during this period. Specifically, other key measures of inter-group inequality in India such as rural-urban gaps Hnatkovska et al. (2024) and gender gaps Bhattacharjee et al. (2015) have also declined sharply since 1983. These trends suggest that important non-caste specific factors may also have been at play.

This paper examines the role of one such non-caste specific factor: the role of aggregate macroeconomic growth. The proximate reason for focusing on growth is the well-known economic liberalization in India in 1991 which sparked a big economic turnaround in a previously moribund economy. Aggregate growth rates rose from an annual average of 3-3.5 percent before 1991 to close to 6 percent in the period since. This growth pick-up was accompanied by an intensifying structural transformation of the economy from agrarian to non-agrarian.

There are important policy implications of this assessment of the role of growth. If growth and the accompanying structural transformation of the economy accounts for a significant share of the caste convergence, then the role of caste-based welfare and affirmative action policies in helping disadvantaged castes catch up becomes much diminished. Put differently, if growth tends to lift all boats, then the policy focus is better aimed at enhancing aggregate growth rather than on group-specific interventions.

We conduct our study by developing a three-sector model (agriculture, manufacturing and services) of an economy with heterogenous agents. Agents differ along two dimensions. First, agents are different in their innate ability endowment which they all draw from a common ability distribution. Second, agents in the model belong to one of two castes: non-SC/STs and SC/STs.

Castes in the model differ on two dimensions: (a) the cost of acquiring schooling; and (b) the cost of accessing sectoral labor markets. These cost differences imply that even though the ability distributions of individuals in the two castes are identical, there is a misallocation of ability which generates caste gaps in sectoral employment and wages. Overall sectoral labor productivity depends both on exogenous productivity as well as worker allocations in education and sectors. Consequently, talent misallocations in the model reduce equilibrium labor productivity while improvements in allocations improve productivity.

We use the model to quantitatively assess the effect of changes in sectoral productivities on schooling and sectoral misallocations during 1983-2012. Specifically, we examine the explanatory power of these productivity changes for the observed decline in the sectoral caste employment gaps, the sectoral caste wage gaps as well as the overall caste wage convergence observed in the data.

The key parameters of the model, including the caste-specific costs of schooling and sectoral

labor market access, are calibrated to match the 1983 levels of the sectoral caste employment gaps, sectoral caste wage gaps and the average education levels of the two castes. Our baseline calibration identifies higher schooling costs for SC/STs as the primary cause of the large sectoral caste gaps in employment and wages in  $1983.^4$ 

Armed with the calibrated model for 1983, we conduct a sequence of quantitative experiments to examine the importance of productivity growth. Our experiments yield two key results. First, exogenous sectoral productivity growth during 1983-2012 induces a decrease in the caste wage gap in the model that is 72 percent of the decline in the data.

Second, we find that a faster increase in the education attainment rates of SC/STs accounts for most of the wage convergence in the model. Intuitively, real costs of schooling decline with aggregate growth. Since SC/STs start with higher costs of schooling in the model, their schooling costs fall proportionately faster with growth. This sparks the relatively faster increase in SC/ST schooling and wages in the model.

The primary driver of the convergence in the model is the decrease in the education costs of SC/STs relative to non-SC/STS. We provide three independent pieces of evidence in support of this mechanism. First, using national and district level education price data we show that (a) the relative price of education fell during this period; and (b) it fell faster in SC/ST dominated districts relative to non-SC/ST dominated districts. Second, we use panel data on states in India for 1983-2012 to show that the cost of schooling (proxied by teacher salaries) rises less than proportionately with per capita incomes.<sup>5</sup> This provides further evidence for declining real costs of education with growth. Third, using census data we show that while initial school provisioning was lower in SC/STs dominated villages in India in 1991, school provisioning increased relatively faster in SC/STs dominated villages during 1991-2011.<sup>6</sup>

<sup>&</sup>lt;sup>4</sup>Higher education costs for SC/STs might seem counterintuitive to the reader since India has had affirmative action programs for education since 1952. These programs provide reserved seats for SC/STs in colleges and universities. Education costs however depend on much more basic things like provisioning of primary, middle and secondary schools. We show below evidence of systematic under-provisioning of schools in SC/ST dominated geographical units, which provides support for SC/STs facing higher schooling costs despite the affirmative action programs.

<sup>&</sup>lt;sup>5</sup>This result echoes a similar finding in the cross-country data reported by Banerjee and Duflo (2005). Teacher salaries represent the largest component of education spending, comprising 80-90 percent of education budgets in advanced countries.

<sup>&</sup>lt;sup>6</sup>One might view the evidence on school provisioning as being indicative of the time costs of schooling in contrast to our model where schooling costs are paid out of goods. However, we show in Online Appendix A that there is an equivalence between our specification of schooling costs being paid in goods and specifications in which schooling costs are paid through time devoted to learning. Crucially, the difference in the goods cost of schooling in our baseline model has a mapping to the difference in the time elasticity of human capital in the time cost formulation. The fact that school provisioning increased faster in SC/ST dominated areas after 1991 is thus consistent with declining schooling costs in both versions.

The education price, the schooling cost and the school provisioning data provide evidence of the key mechanisms embedded in the model: schooling costs are higher for SC/STS; schooling costs of SC/STS declined faster over time than that for non-SC/STs; and that the relative cost of schooling declines with growth.

We interpret our results as suggesting that the rapid growth take-off in India over the past three decades has induced a dramatic narrowing of the historical economic disparities faced by SC/STs. The main force driving this convergence has been the relatively faster increase in the education attainment rates of SC/STs. While other caste-specific policies may have well played a role as well, growth did most of the work by lifting all boats.<sup>7</sup>

The paper is related to three distinct bodies of work. The first is the work on castes in India and their impact on economic outcomes. Aside from the contributions of Hnatkovska et al. (2012) and Hnatkovska et al. (2013) cited above, notable other contributors to this literature are Banerjee and Knight (1985), and Borooah (2005) who examined the discrimination against SC/STs in labor markets in urban India. On a related theme, Ito (2009) studied labor market discrimination in two Indian states – Bihar and Uttar Pradesh. Exploring the theme of castes as networks, Munshi and Rosenzweig (2006) and Munshi and Rosenzweig (2016) show how caste networks impact labor mobility, education choices and employment. Our focus on aggregate caste dynamics and economic growth distinguishes our work from this literature.<sup>8</sup>

A second literature that is related to our work is the extensive work on structural transformation of countries along the development path wherein countries gradually switch their economic focus from agriculture to non-agricultural sectors. This is a voluminous literature that spans both empirical and theoretical work. Key contributions in this are Kongsamut et al. (2001), Ngai and Pissarides (2007) and Acemoglu and Guerrieri (2008). An excellent overview of this literature can be found in Herrendorf et al. (2014). We differ from this work in our focus on the distributional effects of the transformation.

<sup>&</sup>lt;sup>7</sup>Our work also evaluates the relative importance of two other features of the Indian economy. We assess the importance of job reservations for SC/STs in India. Our results suggest that this affirmative action policy may have lowered the *levels* of the caste wage gaps but likely did not qualitatively affect the *dynamics* of caste wage gaps between 1983 and 2012. We also find that the structural transformation that unfolded in the country during this period was important for the caste convergence. The shocks that changed the relative economic shares of the different sectors also changed the sectoral allocation of workers by caste thereby reducing the talent misallocation. Absent this sectoral churn, the misallocations would not have changed similarly.

<sup>&</sup>lt;sup>8</sup>Another paper that is related to our work is Banerjee and Munshi (2004). They examined the differences between entrants belonging to the incumbent traditional community of *Gounders* in the garment industry in Tirupur in India in the early 1990s relative to entrants from other communities. They found evidence of sharp catch-up of capital and output of outsider firms to the levels of entrants from the Gounder community.

Our work also relates to the literature that has examined the effect of labor misallocations on productivity and growth. While this literature is long, the paper closest to our interest is the work on misallocation of talent by Hsieh et al. (2019) who analyze the consequences of misallocating talent by gender and race on productivity and growth in the USA. We share their interest in the implications of misallocating labor due to discrimination or other factors though their focus is on occupational misallocation while we focus on sectoral misallocation.

The next section describes the key facts on caste gaps in India. Section 3 presents the model and some analytical results. Section 4 presents the calibration and quantitative results; Section 5 uncovers the main mechanism at play while 6 provides and some independent evidence in support of the mechanism. Section 7 discusses the importance of structural transformation of the Indian economy and affirmative action policies. The last section concludes.

### 2 Empirical regularities

We start by reporting some aggregate and sectoral facts regarding the wage gaps between SC/STs and non-SC/STs during the period 1983-2012. These facts extend the results reported in Hnatkovska et al. (2012) to 2012 and provide additional cuts of the data. They serve as the empirical motivation of the paper. Our data mainly comes from various rounds of the National Sample Survey (NSS) employment-unemployment household surveys. Details on the data are contained in the Appendix.

Figure 1 reports the wage gaps between the castes across the NSS rounds. Panel (a) shows the mean wage gaps between the groups, while panel (b) shows the corresponding median gaps. The solid lines depict the unconditional wage gaps while the dashed lines show the wage gaps after controlling for the age characteristics of workers.<sup>9</sup> Both plots reveal an unambiguous pattern of wage convergence between the two groups since 1983, with the mean wage gap declining by 10.5% and the median gap falling by 14%.

Given the trends in Figures 1, the natural question to ask is how much of the wage convergence can be explained by measurable worker characteristics like education as well as demographic variables such as age, gender, and location of residence? Hnatkovska et al. (2012) examined this question and found that most of the wage convergence is due to education convergence. We confirm their result during 1983-2012 by using DFL decompositions pioneered by DiNardo et al. (1996).

<sup>&</sup>lt;sup>9</sup>Specifically, to obtain unconditional wage gaps we estimated an OLS regression (for mean) and a Recentered Influence Function (RIF) regression (for median) of log wages on a constant and an SC/ST dummy. The conditional gaps are computed from the same regression with age and age squared controls.

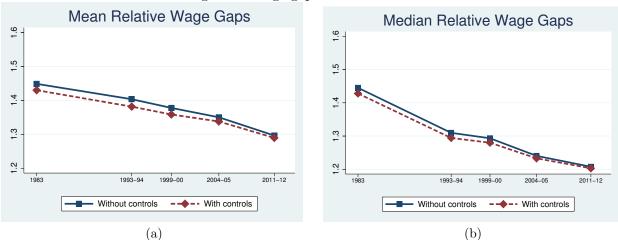


Figure 1: Wage gaps between castes

Notes: Panel (a) of this Figure presents the mean wage gaps between SC/STs and non-SC/STs (expressed as a ratio of non-SC/ST to SC/ST) from the 1983 to the 2011-12 NSS rounds. Panel (b) shows the corresponding median wage gaps. The dashed lines in the two panels show the computed wage gaps after controlling for the age characteristics of workers (age, age squared) while the solid lines are the gaps without such controls.

DFL decompositions consist of constructing a counterfactual wage density for non-SC/STs by re-weighting the non-SC/ST wage density with the distribution of SC/ST attributes of interest. We then compute a percentile wage gap between the actual and counterfactual wage densities for non-SC/STs. This counterfactual percentile wage gap is then compared with the actual percentile gaps from the data to assess the role of the included attributes across the entire wage distribution. The closer the counterfactual wage gap to the actual gaps in the data, the greater is the explanatory power of the included attributes.

Figure 2 shows the DFL decompositions of the wage densities separately for 1983 and 2011-12 as well as the actual percentile wage gaps. For both years, we sequentially introduce three SC/ST attributes – demographic variables (age, age squared, gender, rural sector of residence, and region of residence), education, and state-level affirmative action benefits – to re-weight the non-SC/ST wage density.<sup>10</sup>

There are two main takeaways from Figure 2. First, in both 1983 and 2011-12, education explains over 90 percent of the wage difference between non-SC/STs and SC/STs across the entire distribution. In fact, neither demographics nor affirmative action account for much of the caste

<sup>&</sup>lt;sup>10</sup>We control for regional differences by grouping states into six regions-North, South, East, West, Central, and North-East to reflect similarities across states in their geographic characteristics. Education is introduced through a set of education dummies reflecting education categories 1-5. Affirmative action benefits are proxied by caste reservation quotas.

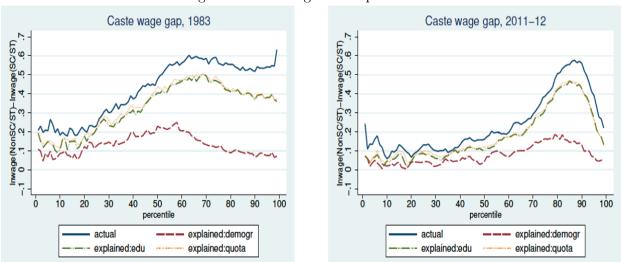


Figure 2: DFL Wage Decomposition

Notes: Blue line is the actual wage gaps at each percentile. Red line is the wage gap explained by *demographic* and *education*. Yellow line is wage gap explained by *demographic* and *education*. Yellow line is wage gap explained by *demographic*, *education*, and *state-level affirmative action*.

wage gap. Second, since the actual percentile wage gap shifted down in 2011-12 relative to 1983 in conjunction with the counterfactual percentile gap given by education, it follows that most of the caste wage convergence in the data is accounted for by education convergence between the groups.

These trends raise the logical question about the deeper reasons behind the observed convergence between the groups during this period since education is clearly an endogenous choice. While there may have been multiple factors operating simultaneously, in this paper we focus on the two biggest changes that occurred in the Indian economy during this period. First, 1983-2012 saw a growth takeoff with average annual per capita GDP growth rising from 3.5 to 6 percent. Second, this period was also marked by a structural transformation of the economy, with agricultural sector contracting and the non-agricultural sectors, in particular services, expanding. See Appendix A.1 for data and figures.

Much of this transformation was associated with rapid productivity growth across sectors as can be seen from Figure 3. Panel (a) shows sectoral output per worker computed from the national accounts data, while panel (b) shows the sectoral labor productivity as reported in the KLEMS dataset for India. All series are normalized by their values in 1983. Both plots of Figure 3 also reveal a common rank-ordering of sectoral labor productivity growth during 1983-2012: manufacturing grew the fastest while agriculture was the slowest growing sector.

So, how did the structural transformation of India's economy affect the two social groups?

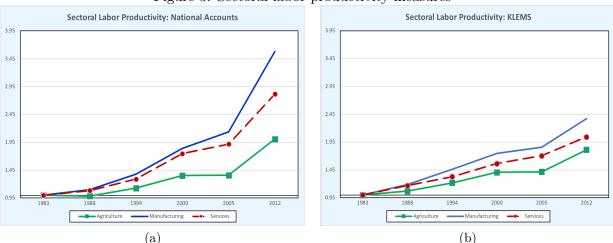


Figure 3: Sectoral labor productivity measures

Notes: Panel (a) of this Figure presents labor productivity, measured as GDP (in constant 1980-81 prices) divided by number of workers in each sector. Panel (b) shows the sectoral labor productivity computed from the KLEMS database for India. All series are normalized by their 1983 values.

Figure 4 reports the industry distribution of SC/ST and non-SC/ST workers, and the relative gaps in this distribution. SC/STs were and remain more likely to be employed in agriculture than non-SC/STs. However the gap narrowed somewhat in the last ten years of our sample. The second largest industry of employment for both social groups is services, whose share has risen steadily over time. Interestingly, services also exhibits the sharpest convergence pattern between non-SC/STs and SC/STs with the relative gap in services employment shares shrinking from 60 percent in 1983 to 21 percent in 2012. Manufacturing shows relatively little change in the employment shares of the two groups over time.

Figures 5 reports the relative gaps in education attainments and median wages between non-SC/STs and SC/STs employed in each sector. The education gaps have narrowed significantly over time between the two caste groups across all sectors. Median wage gaps, on the other hand declined in Services, stayed unchanged in Manufacturing, but widened somewhat in Agriculture.

To summarize, the period 1983-2012 was characterized by high aggregate growth and rising output per worker in all three sectors. There was a gradual transformation of the economy with the services share of both output and employment rising and the agriculture share shrinking. The education gap between the castes declined in all three sectors. While wages were converging *overall* between the castes, there were contrasts in the sectoral patterns: the wage convergence was strong in the service sector but the agricultural sector saw a wage divergence.

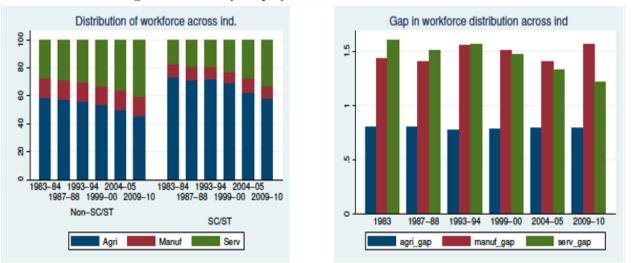
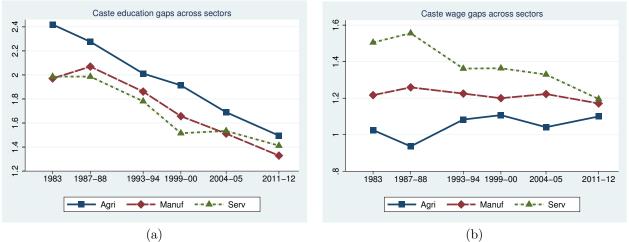


Figure 4: Industry employment distribution across castes

Notes: Panel (a) presents the distribution of workforce across the three industry categories for different NSS rounds. The left set of bars refers to non-SC/STs, while the right set is for SC/STs. Panel (b) presents the ratio of non-SC/STs to SC/STs shares reported in Panel (a) for each industry and year.

Figure 5: Education and wage gaps between non-SC/STs and SC/STs by sector



Notes: Panel (a) presents relative gap in years of education between non-SC/STs and SC/STs in three sectors. Panel (b) presents the ratio of non-SC/STs median wages to SC/STs median wages in three sectors.

### 3 Model

We now ask whether productivity shocks can have a differential impact on the two groups and cause the education and wage gaps between the castes to fall? If so, what are the conditions under which that can happen? Would such an environment also induce sectoral outcomes that are consistent with the facts that we outlined above? Consider a one-period lived closed economy that is inhabited by a continuum of agents of measure L. A measure S of these agents belong to caste s (for scheduled castes and tribes or SC/STs) while a measure N = L - S belong to caste n for non-SC/ST.

Individuals belonging to different castes will be distinct along two margins: the cost of acquiring schooling and the cost of accessing sectoral labor markets. We shall elaborate on each of these features below.

An agent *i* belonging to caste j = n, s maximizes utility from consumption of the final good

$$u\left(c_{ij}\right) = \frac{c_{ij}^{1-\rho}}{1-\rho}$$

Agents produce a final good by combining three intermediate goods using the technology

$$y_{ij} = \left(y_{ij}^a - \bar{y}\right)^{\theta} \left(y_{ij}^m\right)^{\eta} \left(y_{ij}^h\right)^{1-\theta-\eta}$$

where  $y^k$  is intermediate good k = a, m, h. In the following we shall refer to the *a* good as the agricultural good, the *m* good as the manufacturing good and the *h* good as the service-sector good.  $\bar{y}$  is the minimum required level of the *a* good.<sup>11</sup>

Intermediate goods are acquired by agent *i* using her income  $w_i$ . Specifically, an agent *i* of caste j = n, s with income  $w_{ij}$  chooses  $y^a, y^m, y^h$  to maximize production of the final good *y* subject to the budget constraint

$$p^a y^a_{ij} + p^m y^m_{ij} + p^h y^h_{ij} = w_{ij}$$

The optimal expenditures on intermediate goods by an agent i are

$$p^a y^a_{ij} = \theta \left( w_{ij} - p^a \bar{y} \right) + p^a \bar{y} \tag{3.1}$$

$$p^m y_{ij}^m = \eta \left( w_{ij} - p^a \bar{y} \right) \tag{3.2}$$

$$p^{a}y_{ij}^{a} = (1 - \theta - \eta) \left( w_{ij} - p^{a}\bar{y} \right)$$
(3.3)

Substituting the optimal intermediate goods purchases into the production function for the final

<sup>&</sup>lt;sup>11</sup>The general homothetic CES specification induces structural transformation towards the slowest growing sector under the assumption of the elasticity of substitution between sectors being less than one. This has been used by a number of authors to generate the observed structural transformation in the industrial countries (see Ngai and Pissarides (2007) and Acemoglu and Guerrieri (2008)). But that specification would induce a counterfactual expansion of the agricultural sector in India since it was the slowest growing sector during 1983-2012. We proceed with a non-homothetic Cobb-Douglas aggregator instead as it generates the observed structural transformation in India without us having to take a sharp stand on the specific value of the inter-sectoral elasticity of substitution.

good gives

$$y_{ij} = \frac{\theta^{\theta} \eta^{\eta} (1 - \theta - \eta)^{1 - \theta - \eta}}{p^{a\theta} p^{m\eta} p^{h(1 - \theta - \eta)}} (w_{ij} - p^a \bar{y})$$

We define the aggregate price index in this economy (the unit cost of producing the final good) as

$$P = \frac{(p^{a})^{\theta} (p^{m})^{\eta} (p^{h})^{1-\theta-\eta}}{\theta^{\theta} \eta^{\eta} (1-\theta-\eta)^{1-\theta-\eta}}$$
(3.4)

Since we use the final good as the numeraire, with no loss of generality, we set P = 1 throughout the model. Hence, the optimal production of the final good by agent *i* belonging to caste j = n, sis

$$y_{ij} = w_{ij} - p^a \bar{y} \tag{3.5}$$

The non-homotheticity in production of the final good due to a minimum use of the agricultural good will be one source of structural transformation in the model.

#### 3.1 Ability and Human Capital

Each agent is born with an endowment of ability  $a_i$  and one unit of labor time that is supplied inelastically to the labor market. Ability is drawn from an *i.i.d.* process that follows the cumulative distribution function G(a),  $a \in [\underline{a}, \overline{a}]$ . The ability distribution is identical for both castes.

Ability is a productive input in building human capital. Human capital, in turn, determines the agent's labor productivity as well as the cost of accessing sector specific labor markets. Specifically, human capital of an agent i is determined by

$$e_{ij} = a_{ij} q_{ij}^{\chi}, \ \chi \in (0,1) \tag{3.6}$$

where q is schooling acquired by the agent and  $\chi$  denotes the schooling elasticity of human capital.

Acquiring human capital is expensive with the cost of acquiring q units of schooling being  $\lambda_j q$ where  $\lambda_j$ , j = n, s is the marginal cost of schooling which is denominated in terms of the final good. Note that the marginal cost of education is constant and caste specific. This is the first difference between individuals belonging to different castes.

#### **3.2** Human Capital and Sectoral Employment

An agent can work in any of the three sectors conditional on paying the entry costs of accessing those sectors.<sup>12</sup> With no loss of generality, we normalize the entry cost in sector-*a* to zero. Access to sectors *m* and *h* however are costly. Agent *i* can access sector-k = m, h by spending  $f_{ij}^k$  units of the final good. Notice that this specification allows the sectoral entry costs to be caste specific.

In what follows we shall make the following assumptions:

Assumption 1:

$$f_{ij}^{k} = \begin{cases} 0, & k = a; \ j = n, s \\ \phi(\gamma_{j}^{k} - \alpha e_{ij}), & k = m, h; \ j = n, s \end{cases}$$

**Assumption 2**:  $\gamma_j^h > \gamma_j^m, \quad j = n, s$ 

Assumption 1 says that sectoral entry costs only apply for entry into sectors m and h. The entry costs have two components. The first,  $\gamma_j^k$ , is a fixed cost that is specific to sector and caste. The second component,  $\alpha e_{ij}$ , is decreasing in the human capital of the individual but where the marginal effect of human capital on the entry cost is identical across castes.  $\phi$  is a scaling factor that has no qualitative effect on the results but is useful for quantitative purposes.<sup>13</sup>

Assumption 2 implies that the fixed cost of entry into sector-h is greater than the entry cost for sector-m for both castes. This ensures an ability rank order where the highest ability individuals work in sector-h (consistent with the evidence on the sectoral distribution of human capital).

The preceding makes clear that there are two fundamental sources of differences across castes: the cost of education  $\lambda$  and the fixed costs of entry into sectors m and h. We shall explore the implications of these differences below.

<sup>&</sup>lt;sup>12</sup>We view the entry cost as a way to capture a combination of sectorial discrimination against particular caste, caste-base networks as in Munshi and Rosenzweig (2006) and Munshi and Rosenzweig (2016), and the constitutionally mandated affirmative action policies that make entry into public sector jobs easier for SCSTs. One can imagine the discrimination and networks may make the entry costs for SCST relatively higher than that for the NST workers, whereas affirmative actions work oppositely. In light of this, we do not take a stand on which caste group has a higher entry cost and leave these costs to be calibrated freely in our quantitative analysis.

<sup>&</sup>lt;sup>13</sup>The second component of the sectoral entry cost,  $\alpha e_{ij}$ , is not required for any of the qualitative results on caste gaps that we derive below. However, we allow for this second term, which is independent of caste, to allow for the fact that schooling creates network of connections that is broader than the individual's immediate family and caste connections or networks.

#### 3.3 Sectoral Production Technologies

The technologies for producing the three goods are all linear in the human capital of the worker. In particular, a worker with ability  $e_i$  supplying one unit of labor time to sector a produces

$$y_i^a = Ae_i$$

An *m*-sector worker with ability  $e_i$  produces the manufacturing good *m* according to

$$y_i^m = Me_i$$

Lastly, an h-sector worker with ability  $e_i$  produces the service sector good according to

$$y_i^h = He_i$$

Note that labor supply is inelastic and indivisible. So each worker supplies one unit of labor time to whichever sector she works in.

#### **3.4** Sector and Schooling Choice

The decisions about which sector to work in and what human capital level to acquire are joint in this model since the schooling decision is contingent on the returns to human capital which, in turn, is dependent on the sector of employment of the worker since human capital impacts both the direct returns to work as well as the sectoral entry costs.

#### 3.4.1 The schooling choice

An agent belonging to caste j = n, s who intends to work in sector-*a* will choose schooling *q* to maximize to maximize consumption:

$$c^a_{ij} = y^a_{ij} - \lambda_j q_{ij}$$

Similarly, an agent planning to work in sector-m will choose her schooling to maximize

$$c_{ij}^{m} = y_{ij}^{m} - \lambda_{j} q_{ij} - \phi \left( \gamma_{j}^{m} - \alpha a_{ij} q_{ij}^{\chi} \right)$$

while an agent headed for work in sector-h would choose schooling q to maximize

$$c_{ij}^{h} = y_{ij}^{h} - \lambda_{j} q_{ij} - \phi \left( \gamma_{j}^{h} - \alpha a_{ij} q_{ij}^{\chi} \right)$$

where  $y_{ij}^k = w_{ij}^k - p^a \bar{y}, k = a, m, h.$   $w_{ij}^k$  denotes wages for the individual contingent on the sector that she chooses to work in. These sectoral wages are given by

$$w_{ij}^{k} = \begin{cases} p^{a} A a_{ij} \left( q_{ij}^{a} \right)^{\chi} \text{ if } i \text{ works in } a \\ p^{m} M a_{ij} \left( q_{ij}^{m} \right)^{\chi} \text{ if } i \text{ works in } m \\ p^{h} H a_{ij} \left( q_{ij}^{h} \right)^{\chi} \text{ if } i \text{ works in } h \end{cases}$$

Notice that the schooling choice contingent on working in sector k = a, m, h internalizes the effects of schooling on the sectoral entry costs.

The optimal schooling choices for an agent *i* belonging to caste *j* who chooses to work in sector-k = a, m, h are:

$$q_{ij}^a = \left(\frac{\chi a_{ij} p^a A}{\lambda_j}\right)^{\frac{1}{1-\chi}} \tag{3.7}$$

$$q_{ij}^m = \left(\frac{\chi a_{ij} \left(p^m M + \phi \alpha\right)}{\lambda_j}\right)^{\frac{1}{1-\chi}}$$
(3.8)

$$q_{ij}^{h} = \left(\frac{\chi a_{ij} \left(p^{h} H + \phi \alpha\right)}{\lambda_{j}}\right)^{\frac{1}{1-\chi}}$$
(3.9)

The optimal schooling functions above reflect two key features. First, within each sector higher ability agents acquire more schooling and hence, greater human capital. Second, controlling for ability, sectors with higher labor productivity will have workers with greater human capital since schooling is increasing in sectoral productivity.

#### 3.4.2 Sectoral employment choice

The decision regarding the sector of employment is then based on choosing the sector associated with the highest consumption:  $max \left\{c_{ij}^a, c_{ij}^m, c_{ij}^h\right\}$  where  $c_{ij}^k$  denotes the consumption of an agent iof caste j working in sector k = a, m, h. Since both schooling and sectoral entry costs are paid out of the household final good, the household budget constraint dictates that  $c_{ij}^k = y_{ij}^k - \lambda_j q_{ij}^k - f_{ij}^k$ where  $y_{ij}^k$  is given by equation 3.5 and  $f_{ij}^k$  is given by Assumption 1. The sector-specific schooling levels in equations 3.7-3.9 above imply consumption levels for agents contingent on their decisions regarding schooling and sector of employment:

$$c_{ij}^{a} = (1-\chi) \left(\frac{\chi}{\lambda_j}\right)^{\frac{\chi}{1-\chi}} (a_{ij}p^a A)^{\frac{1}{1-\chi}} - p^a \bar{y}$$
(3.10)

$$c_{ij}^{m} = (1 - \chi) \left(\frac{\chi}{\lambda_j}\right)^{\frac{\Lambda}{1-\chi}} \left\{ a_{ij} \left( p^m M + \phi \alpha \right) \right\}^{\frac{1}{1-\chi}} - \phi \gamma_j^m - p^a \bar{y}$$
(3.11)

$$c_{ij}^{h} = (1 - \chi) \left(\frac{\chi}{\lambda_{j}}\right)^{\frac{\chi}{1 - \chi}} \left\{ a_{ij} \left( p^{h} H + \phi \alpha \right) \right\}^{\frac{1}{1 - \chi}} - \phi \gamma_{j}^{h} - p^{a} \bar{y}$$
(3.12)

As in the schooling decisions, consumption of agents is also increasing in their ability a within each sector. Note that the consumption levels associated with working in each sector are net of the costs of schooling and sectoral entry costs since those are paid by the agent out of the household final good  $y_{ij}$ .

To describe the distribution of agents into the different sectors it is useful to define three ability thresholds:

$$\hat{a}_{j}^{m} = \left[\frac{\phi\gamma_{j}^{m}}{\left(1-\chi\right)\left(\frac{\chi}{\lambda_{j}}\right)^{\frac{\chi}{1-\chi}}\left\{\left(p^{m}M+\phi\alpha\right)^{\frac{1}{1-\chi}}-\left(p^{a}A\right)^{\frac{1}{1-\chi}}\right\}}\right]^{1-\chi}$$
(3.13)

$$\hat{a}_{j}^{h} = \left[\frac{\phi\gamma_{j}^{h}}{\left(1-\chi\right)\left(\frac{\chi}{\lambda_{j}}\right)^{\frac{\chi}{1-\chi}}\left\{\left(p^{h}H + \phi\alpha\right)^{\frac{1}{1-\chi}} - \left(p^{a}A\right)^{\frac{1}{1-\chi}}\right\}}\right]^{-\chi}$$
(3.14)

$$\tilde{a}_j^h = \left[\frac{\phi(\gamma_j^h - \gamma_j^m)}{\left(1 - \chi\right)\left(\frac{\chi}{\lambda_j}\right)^{\frac{\chi}{1 - \chi}} \left\{ (p^h H + \phi\alpha)^{\frac{1}{1 - \chi}} - (p^m M + \phi\alpha)^{\frac{1}{1 - \chi}} \right\}}\right]^{1 - \chi}$$
(3.15)

Equation 3.13 defines the threshold ability level  $\hat{a}^m$  for which consumption from working in sectora is the same as consumption from working in sector-m, i.e.,  $c_{ij}^a = c_{ij}^m$ . Hence, an agent with ability  $\hat{a}^m$  is indifferent between working in sector-a or sector-m.  $\hat{a}^h$  and  $\tilde{a}^h$  give the corresponding indifference between sectors-a and h, and between sectors m and h, respectively.

We now make the following assumption to provide greater structure to the cross-sectoral distribution of ability and skills that the model can generate:

Assumption 3: Parameter values guarantee  $p^{h}H + \phi \alpha > p^{m}M + \phi \alpha > p^{a}A$ 

Assumption 3 is necessary (but not sufficient) for there to be a distribution of abilities across all

three sectors. This will become clearer in the analysis below.

The thresholds along with Assumptions 1-3 allow a clear pairwise ranking of sectors for each ability type. This is summarized in the following Lemma:

**Lemma 3.1.** All individuals  $i \in \text{caste } j = n, s$  with ability  $a_{ij}$  prefer employment in sector-m to employment in sector-a if  $a_{ij} \ge \hat{a}_j^m$ ; employment in sector-h to sector-a if  $a_{ij} \ge \hat{a}_j^h$ ; and employment in sector-h to sector-m if  $a_{ij} \ge \tilde{a}_j^h$ .

Proof. See Appendix.

#### 3.4.3 Mapping Abilities to Sectors

How do agents get distributed across sectors in this economy? This depends on the relative rank ordering of the three thresholds  $\hat{a}_j^m$ ,  $\hat{a}_j^h$ , and  $\tilde{a}^h$ . The following lemma is useful for characterizing the different possibilities:

Lemma 3.2. The rank order of the three ability thresholds are

$$\begin{split} \tilde{a}_j^h < \hat{a}_j^h < \hat{a}_j^m & \text{if } \hat{a}_j^h = \min[\hat{a}_j^m, \hat{a}_j^h] \\ \tilde{a}_j^h > \hat{a}_j^h > \hat{a}_j^m & \text{if } \hat{a}_j^h = \max[\hat{a}_j^m, \hat{a}_j^h] \end{split}$$

Proof. See Appendix.

Lemma 3.2 describes the relationship between the three thresholds in the model. Specifically, it says that  $\tilde{a}_j^h$  cannot lie in between  $\hat{a}_j^m$  and  $\hat{a}_j^h$ . Rather, it lies on the same side of  $\hat{a}_j^m$  as  $\hat{a}_j^h$ .

Since the model structure can give rise to  $\hat{e}^h \ge \hat{e}^m$ , the following Proposition characterizes the mapping of the abilities to sectoral employment under both these cases:

**Proposition 3.1.** (a) When  $\hat{a}_j^h > \hat{a}_j^m$ , j = n, s, the sectoral distribution of abilities is

$$a_{i} \in \begin{cases} [\underline{a}_{j}, \hat{a}_{j}^{m}) & : i \in A \\ [\hat{a}_{j}^{m}, \tilde{a}_{j}^{h}) & : i \in M \\ [\tilde{a}_{j}^{h}, \bar{a}_{j}] & : i \in H \end{cases}$$

b) When  $\hat{a}_j^h < \hat{a}_j^m$ , j = n, s, the sectoral distribution of abilities is

$$a_i \in \begin{cases} [\underline{a}_j, \hat{a}_j^h) & : i \in A \\ [\hat{a}_j^h, \hat{a}_j^m) & : i \in H \\ [\hat{a}_j^m, \bar{a}_j] & : i \in H \end{cases}$$

*Proof.* (a) When  $\hat{a}_j^m < \hat{a}_j^h$ , Lemma 3.2 says that we must have  $\hat{a}_j^m < \hat{a}_j^h < \tilde{a}_j^h$ . The distribution of ability types across the three sectors in this case follows directly from equations 3.13, 3.14, 3.15, and Lemma 3.1. Ability types below  $\hat{a}_j^m$  work in sector-*a* while those in between  $\hat{a}_j^m$  and  $\hat{a}_j^h$  choose sector-*m*. For ability types between  $\hat{a}_j^h$  and  $\tilde{a}_j^h$ , equation 3.15 implies that employment in sector-*m* is strictly preferred to sector-*h*. Those with ability above  $\tilde{a}_j^h$  choose to work in sector-*h*, which follows directly from equation 3.15.

(b) When  $\hat{a}_j^h < \hat{a}_j^m$ , from Lemma 3.2 we have  $\tilde{a}_j^h < \hat{a}_j^h < \hat{a}_j^m$ . In this case, the distribution of ability types across sectors follows directly from equations 3.13-3.14 and Lemma 3.1. Ability types below  $\hat{a}_j^h$  strictly prefer employment in sector-*a* to both sectors *h* and *m*. For all ability types in caste j = n, s with  $a \in [\hat{a}_j^h, \hat{a}_j^m)$ , employment in sector-*h* dominates both sectors *a* and *m*. For  $a \ge \hat{a}_j^m > \tilde{a}_j^h$ , equation 3.13 says that sector-*m* dominates sector-*a* while equation 3.15 says that working in sector-*h* is strictly preferred by these types over sector-*m* employment.

While the message of Proposition 3.1 is self-explanatory, a comment on part (b), which describes allocations when  $\hat{a}_j^h < \hat{a}_j^m$ , is useful. The ability distribution described in Proposition 3.1 for this case implies that labor from both castes choose employment in either sector-*a* or sector-*h*, thereby rendering sector-*m* empty. This is clearly counterfactual since our data analysis revealed that both castes were employed in all three sectors. In the remainder of the paper we ignore this case and focus exclusively on parameter configurations such that  $\hat{a}_j^h > \hat{a}_j^m$  for  $j = n, s.^{14}$ 

#### 3.5 Market clearing and Equilibrium

Markets for each good must clear individually. For the intermediate goods, this implies that total production must equal total demand for each good individually:

$$Y^{a} = L\left[s\int_{\underline{a}}^{\overline{a}} y^{a}_{is}dG(a) + n\int_{\underline{a}}^{\overline{a}} y^{a}_{in}dG(a)\right]$$
(3.16)

<sup>&</sup>lt;sup>14</sup>The case  $\hat{a}_j^h = \hat{a}_j^m = \tilde{a}_j^j$  is possible but clearly non-generic. Consequently, we ignore this pathological possibility.

HNATKOVSKA-HOU-LAHIRI: CASTE CONVERGENCE

$$Y^m = L\left[s\int_{\underline{a}}^{\overline{a}} y^m_{is} dG(a) + n\int_{\underline{a}}^{\overline{a}} y^m_{in} dG(a)\right]$$
(3.17)

$$Y^{h} = L \left[ s \int_{\underline{a}}^{\overline{a}} y^{h}_{is} dG(a) + n \int_{\underline{a}}^{\overline{a}} y^{h}_{in} dG(a) \right]$$
(3.18)

where  $Y^k$  denotes total production of intermediate good k = a, m, h. Note that in equations 3.16-3.18, sectoral output of individual *i* belonging to caste j = n, s whose ability is outside the relevant sectoral ability thresholds given in Proposition 3.1 will be zero.

Total production of the final good must equal the total demand for the final good:

$$C + Q + F = Y = L \left[ s \int_{\underline{a}}^{\overline{a}} y_{is} dG(a) + n \int_{\underline{a}}^{\overline{a}} y_{in} dG(a) \right]$$
(3.19)

where Q denotes total costs of schooling by all workers, F denotes the total skill acquisition costs incurred by workers employed in sector m and sector h, while Y denotes total production of the final good by all agents. The market clearing condition for the m good recognizes that part of the use of the good is for acquiring skills.

DEFINITION: The Walrasian equilibrium for this economy is a vector of prices  $\{p_m, p_h\}$  and quantities  $\{Y^a, Y^m, Y^h, C_s, C_n, Q_s, Q_n, F^m, F^h, \hat{a}_s^m, \hat{a}_s^h, \hat{a}_n^m, \hat{a}_n^h\}$  such that all worker-households satisfy their optimality conditions, budget constraints are satisfied and all markets clear.

#### 3.6 Sectoral Labor and Wage Gaps Between Castes

It is useful at this stage to describe the caste labor gaps and wage gaps in the three sectors since those are a key object of interest. The precise expressions for these gaps depend on the specifics of the underlying distribution from which individuals draw their ability endowment. Throughout the rest of the paper we shall maintain the assumption that the ability distribution is uniform:

**Assumption** 4: The ability distribution G(a) is uniform on the support  $[\underline{a}, \overline{a}]$ .

The labor employment gap between caste n and caste s in sector k = a, m, h is the ratio of the fraction of caste n workers employed in sector k to the fraction of caste s workers employed in sector k. Under Assumption 4, these gaps are given by:

$$\Delta s^a = \frac{\hat{a}_n^m - \underline{a}}{\hat{a}_s^m - \underline{a}} \tag{3.20}$$

$$\Delta s^m = \frac{\tilde{a}_n^h - \hat{a}_n^m}{\tilde{a}_s^h - \hat{a}_s^m} \tag{3.21}$$

$$\Delta s^h = \frac{\bar{a} - \tilde{a}_n^h}{\bar{a} - \tilde{a}_s^h} \tag{3.22}$$

To derive the sectoral caste wage gaps from the model, note that the ability thresholds and the sector-contingent schooling choices given by equations 3.7-3.9 imply that the mean sectoral wages of agents belonging to caste j = n, s are

$$\begin{split} w_j^a &= (p^a A)^{\frac{1}{1-\chi}} \left(\frac{\chi}{\lambda_j}\right)^{\frac{\chi}{1-\chi}} \int_{\underline{a}}^{\hat{a}_j^m} a^{\frac{1}{1-\chi}} \frac{dG(a)}{G(\hat{a}_j^m)} \\ w_j^m &= p^m M \left(p^m M + \phi \alpha\right)^{\frac{\chi}{1-\chi}} \left(\frac{\chi}{\lambda_j}\right)^{\frac{\chi}{1-\chi}} \int_{\hat{a}_j^m}^{\tilde{a}_j^h} a^{\frac{1}{1-\chi}} \frac{dG(a)}{G(\tilde{a}_j^h) - G(\hat{a}_j^m)} \\ w_j^h &= p^h H \left(p^h H + \phi \alpha\right)^{\frac{\chi}{1-\chi}} \left(\frac{\chi}{\lambda_j}\right)^{\frac{\chi}{1-\chi}} \int_{\tilde{a}_j^h}^{\bar{a}} a^{\frac{1}{1-\chi}} \frac{dG(a)}{1 - G(\tilde{a}_j^h)} \end{split}$$

Since the caste wage gap in sector k = a, m, h is the ratio of the mean wage of caste n relative to the mean wage of caste s in sector k, the sectoral caste wage gaps under Assumption 4 are given by:

$$\Delta w^{a} = \left(\frac{\lambda_{s}}{\lambda_{n}}\right)^{\frac{\chi}{1-\chi}} \left(\frac{(\hat{a}_{n}^{m})^{\frac{1}{1-\chi}+1} - (\underline{a})^{\frac{1}{1-\chi}+1}}{(\hat{a}_{s}^{m})^{\frac{1}{1-\chi}+1} - (\underline{a})^{\frac{1}{1-\chi}+1}}\right) \left(\frac{\hat{a}_{s}^{m} - \underline{a}}{\hat{a}_{n}^{m} - \underline{a}}\right)$$
(3.23)

$$\Delta w^{m} = \left(\frac{\lambda_{s}}{\lambda_{n}}\right)^{\frac{\chi}{1-\chi}} \left(\frac{(\tilde{a}_{n}^{h})^{\frac{1}{1-\chi}+1} - (\hat{a}_{n}^{m})^{\frac{1}{1-\chi}+1}}{(\tilde{a}_{s}^{h})^{\frac{1}{1-\chi}+1} - (\hat{a}_{s}^{m})^{\frac{1}{1-\chi}+1}}\right) \left(\frac{\tilde{a}_{s}^{h} - \hat{a}_{s}^{m}}{\tilde{a}_{n}^{h} - \hat{a}_{n}^{m}}\right)$$
(3.24)

$$\Delta w^{h} = \left(\frac{\lambda_{s}}{\lambda_{n}}\right)^{\frac{\chi}{1-\chi}} \left(\frac{\bar{a}^{\frac{1}{1-\chi}+1} - (\tilde{a}^{h}_{n})^{\frac{1}{1-\chi}+1}}{\bar{a}^{\frac{1}{1-\chi}+1} - (\tilde{a}^{h}_{s})^{\frac{1}{1-\chi}+1}}\right) \left(\frac{\bar{a} - \tilde{a}^{h}_{s}}{\bar{a} - \tilde{a}^{h}_{n}}\right)$$
(3.25)

where the thresholds  $\hat{a}_j^m, \tilde{a}_j^h$  are given by equations 3.13 and 3.15, respectively.

The wage and labor expressions above make clear that the key variables that determine the sectoral caste gaps in the model are the ability thresholds  $\hat{a}_j^m$  and  $\tilde{a}_j^h$  for j = n, s. The differences in the ability thresholds across the castes, in turn, depend on differences in schooling costs and sectoral entry costs. This follows directly from equations 3.13 and 3.15 which can be used to get

$$\frac{\hat{a}_n^m}{\hat{a}_s^m} = \left(\frac{\lambda_n}{\lambda_s}\right)^{\chi} \left(\frac{\gamma_n^m}{\gamma_s^m}\right)^{1-\chi} \tag{3.26}$$

$$\frac{\tilde{a}_n^h}{\tilde{a}_s^h} = \left(\frac{\lambda_n}{\lambda_s}\right)^{\chi} \left(\frac{\gamma_n^h - \gamma_n^m}{\gamma_s^h - \gamma_s^m}\right)^{1-\chi} \tag{3.27}$$

These results show that the ability thresholds as well as the education and employment distributions differ across the castes in the model despite members of the two castes drawing from the same ability distribution. These caste gaps arise due to differences in the costs of schooling and the sectoral entry fixed costs which are the only sources of difference across castes in the model.

#### 3.7 Goods cost versus time cost for schooling

We have modelled schooling costs as being paid out of the final good. An alternative would be for schooling costs to be in the form of time needed to get educated. In Online Appendix A, we explore two alternative formulations with time costs or both time and goods costs for schooling. We show that both these alternative versions have the same features as in the goods cost version. In particular, an individual's human capital and consumption are increasing in aggregate productivity and individual ability. Crucially, we show that there exist parameter configurations that render outcomes in the alternative versions isomorphic.

The equivalence between the time cost and goods cost versions of the model arises from the fact that the elasticity of human capital with respect to schooling time has a mapping to the goods cost of education. Specifically, a lower time elasticity of human capital implies greater foregone goods production. Hence, in our example, the model with time costs of schooling can be rewritten as a model with goods costs of education with a suitable specification of the goods cost parameter in terms of the time elasticity parameter. Importantly, the difference between the caste groups in their education costs has an analogue in the difference in the time elasticity of human capital: SC/STs would have a lower time elasticity of human capital relative to non-SC/STs.

We chose the goods cost formulation for schooling primarily due to the absence of detailed time use data to measure the time spent in school. Since we have access to disaggregated expenditure data, price data, as well as sectoral productivity data, it is easier to map the goods cost version to the data. However, we also show suggestive evidence on the time costs of education in India during this period and how they have declined relatively faster for SC/STs during the post-1983 period.

### 4 A Quantitative Evaluation

We now turn to a quantitative implementation of the full version of the three-sector model. Specifically, we examine whether a calibrated version of the three sector model can explain the observed caste gap dynamics through the observed macroeconomic growth; and whether the caste education subsidization in India through reservations were crucial for the observed convergence.

The quantitative strategy of this section is to calibrate the model to the mimic the 1983 distribution of education, sectoral employment and sectoral wage of the two castes. Next, we identify the sectoral productivity changes between 1983 and 2012 by matching the change in sectoral labor productivities in the model with the corresponding changes in the sectoral output per unit labor reported in the National Income and Product Accounts data. We then feed the estimated paths of sectoral productivity into the calibrated model. The resulting distributional implications of the model at each date are then compared to the data in order to evaluate the explanatory power of aggregate productivity shocks for the caste wage gap dynamics.

Table 1: Calibration of Key Variables						
VARIABLE	VARIABLE VALUE VARIABLE					
$\bar{y}$	0.5	$\theta$	0.46			
$\eta$	0.15	$\alpha$	1			
<u>a</u>	1	$\bar{a}$	50			
$\frac{\underline{a}}{\underline{M}}$	1.2	$\frac{H}{A}$ 1983	1.1			
L	1	$\overset{11333}{S}$	0.25			
Calibrated variables						
$\gamma_s^m$ 20.1360 $\gamma_s^h$ 299.1381						
$\frac{\overline{\gamma_s^m}}{\frac{\gamma_n^m}{\gamma_s^m}}$	1.036	$rac{\gamma_n^h-\gamma_n^m}{\gamma_s^h-\gamma_s^m}$	1.332			
$\frac{\lambda_s}{\lambda_n}$	1.55	$\phi$	0.53			
$\lambda_s$	2.53	$\chi$	0.61			
Notes: The table gives the parameters used for cali-						
brating the model. The top papel lists the parameter						

brating the model. The top panel lists the parameter values that were taken from other studies. The parameters in the bottom panel of the table were picked to match data moments from 1983.

Our focus is on eight key data moments for 1983: the three sectoral caste employment gaps; the three sectoral caste wage gaps; and the two average education levels  $\bar{q}_n$  and  $\bar{q}_s$ . Our calibration strategy is to match these eight data moments by choosing the following eight parameters: the sectoral entry cost parameters  $\left(\gamma_s^m, \gamma_s^h, \frac{\gamma_m^m}{\gamma_s^m}, \frac{\gamma_n^h}{\gamma_s^h}\right)$ , the two education cost parameters  $\left(\frac{\lambda_n}{\lambda_s}, \lambda_s\right)$ , the scaling parameter  $\phi$  and the schooling elasticity of human capital  $\chi$ .

Table 1 reports the key parameters. The upper panel of the table gives the parameters that were either normalizations or values that were taken from other studies. The numbers in the lower panel are the ones that were calibrated to match the moments of the 1983 caste distribution.

There are three features to note about the calibration parameters in Table 1. First, in order to

match the sectoral caste gaps in 1983 the model demands that  $\frac{\lambda_s}{\lambda_n} = 1.55$  so that the schooling costs for caste-*s* are 55 percent higher than that for caste-*n*. This feature allows the model to match the fact that SC/STs are over-represented in sector-*a*. The higher cost of schooling limits their access to the non-agricultural sectors.<sup>15</sup>

Second, the entry cost for services exceeds the entry cost for manufacturing for both SC/STs and non-SC/STs is for services, i.e.,  $\gamma_k^h > \gamma_k^m$ , k = n, s. This reflects the fact that average years of schooling of service sector workers is greater than the average schooling years of manufacturing workers in all our sample rounds. Figure 6 in the Appendix shows this. In other words, despite the wide variance of skill levels across the various types of services, the average skill level of service sector workers is still greater than that of manufacturing workers.

Third, matching the caste gaps in 1983 also requires the fixed costs of entry into sectors m and h to be lower for caste-s. These are consistent with the presence of affirmative action programs that provide reservations for SC/STs in public sector jobs, which are mostly in the non-agricultural sectors. From the model perspective, given the schooling gap between SC/STs and non-SC/STs, the model would predict counterfactually few SC/STs in the higher skill sectors. The higher schooling costs faced by SC/STs would also *reduce* the average wage gap in manufacturing and services since only the most high ability and highly educated SC/STS would work in those sectors. But that is counterfactual since the wage gaps in these two sectors are higher than in agriculture. Having lower sectoral entry costs for SC/STs in manufacturing and services allows the model to simultaneously match the sectoral employment and wage gaps between the castes in the data.

Our quantification strategy is to freeze the calibrated parameters at the 1983 values and recompute the equilibrium by feeding in the identified change in the exogenous sectoral productivities A, M, H between 1983 and 2012.<sup>16</sup> Note that since the model has no intrinsic dynamics, each new level for productivity generates a new equilibrium.

Given the specification of our model, one cannot compute the exogenous sectoral productivities from the sectoral labor productivities reported in the National Income accounts. In the model, agents endogenously acquire human capital through schooling and also choose their sector of em-

<sup>&</sup>lt;sup>15</sup>The higher schooling costs for SC/STs reduces the share of SC/ST who transit to the higher skill sectors, thereby raising the average ability of SC/STs in agriculture. However the lower levels of schooling of the SC/STs who remain in Agriculture lowers the labor productivity of SC/ST workers in Agriculture enough to allow the model to simultaneously generate  $\Delta s^A < 1$  and  $\Delta w^A > 1$ .

<sup>&</sup>lt;sup>16</sup>An alternative approach would be to change education and entry costs as well as productivity growth in 2012. This approach allows for both exogenous changes in the costs and the endogenous changes of these costs through the impact of growth. We perform this exercise in Online Appendix B. The results suggest that growth plays a dominant role in creating both wage and education convergence as observed in the data.

ployment. This educational and sectoral sorting impacts their productivity. Consequently, sectoral labor productivity reflects the joint effects of exogenous sectoral productivity, endogenous human capital of the sectoral labor force and the endogenous sectoral sorting by workers. This is true both in the data and the model.

We approach the problem in a hybrid way. We first estimate sectoral productivities in 1983 by running sectoral Mincer wage regressions on five categories of education attainment of workers (primary, middle, secondary, college, diploma/technical) and a constant using the NSS employment/unemployment household survey for 1983. We use the constant in these sectoral wage regressions as our estimates of sectoral productivity in 1983. These numbers for relative sectoral productivities are reported in the top panel of Table 1.

To get the growth rates between 1983 and 2012 of the exogenous sectoral productivities A, M, and H, we first fix the calibrated parameters at 1983 level. We then pick the exogenous sectoral productivity growth rates such that the implied growth rates of sectoral output per worker between 1983 and 2012 in the model exactly match the corresponding growth rates in the data.<sup>17</sup> This procedure yields the following sectoral productivity growth rates<sup>18</sup>:

 $g_A = 1.1436$   $g_M = 2.1421$   $g_H = 2.4068$ 

Table 2 shows the match between the eight targeted variables and their corresponding data values in 1983. The model clearly matches the rank order and magnitudes of the targeted moments for the sectoral caste gaps in both labor shares and wages gaps. It also does well in matching the mean education levels of the two castes in 1983, though the fit is not quite as precise as that for the six sectoral caste gaps.<sup>19</sup>

How well does the model perform with respect to the non-targeted moments for the two castes in 1983? The bottom panel of Table 2 shows the fit of the model with respect to three non-targeted caste gaps. The first is the one that is the main object of the paper: the overall caste wage gap. The model generates a relative wage premium for non-SC/STs of 34 percent. Relative to the 45

<sup>&</sup>lt;sup>17</sup>In our data analysis, labor productivity is computed as average output per worker for each sector in 1983 prices whose model counterpart is  $Ey^k = \frac{p_{83}^k Y^k}{L^k}$  k = a, m, h where  $Y^k$  is given by (3.16)-(3.18),  $p_{83}^k$  is price levels at 1983, and  $L^k$  is the measure for employment in sector k.

<sup>&</sup>lt;sup>18</sup>The fact that the estimated agricultural labor productivity growth in India during 1983-2012 is the lowest amongst the three sectors is a pattern that is echoed also in the growth of overall sectoral output per worker during this period. We expand on these sectoral productivities and their implications for sectoral prices in Section C below.

<sup>&</sup>lt;sup>19</sup>Schooling in the model is a continuous variable whereas in the data it is in years of schooling. To compare the schooling statistics in the model with the data, we normalize both the model and the data education series by de-meaning them. The statistics reported in Table 2 are computed using these de-meaned series.

			-		
		1983		2012	
VARIABLE	Notation	Data	Model	Data	Model
		TARGETED		Non-Targeted	
Wage Gap Agriculture	$\Delta w^a$	1.04	1.04	1.08	1.05
Wage Gap Manufacture	$\Delta w^m$	1.20	1.20	1.14	1.20
Wage Gap Service	$\Delta w^h$	1.45	1.45	1.33	1.16
Labor Share Gap Agri	$\Delta s^a$	0.80	0.85	0.79	0.85
Labor Share Gap Manuf	$\Delta s^m$	1.43	1.43	1.57	2.15
Labor Share Gap Serv	$\Delta s^h$	1.61	1.60	1.21	1.32
Mean educ $SC/ST$	$ar{q}_s$	1.81	1.75	4.73	3.78
Mean educ Non-SC/ST	$ar{q}_n$	4.08	3.86	5.78	6.59
		Non-Targeted		Non-Targeted	
Total wage gap	$\Delta w$	1.45	1.34	1.30	1.24
Pareto shape para: Schooling SC/ST	$k_s$	0.57	0.77	1.33	1.19
Pareto shape para: Schooling Non-SC/ST	$k_n$	1.12	1.16	1.52	1.58
	. 1		• •	. 1	

Table 2: Data and Model Moments

Notes: The top panel of the table reports the sectoral caste gaps in employment and wages with all gaps being the ratio of Non-SC/ST to SC/ST. The bottom panel reports the data and model generated of selected non-targeted moments.

percent non-SC/ST wage premium in the data, we consider the fit to be quite good.

The model allows for heterogeneity both within and across groups. To examine the fit of the model with regard to its predicted heterogeneity, we first fit a Pareto distribution to the years of schooling of agents separately for each caste in the NSS household survey data for 1983. We then do the same to the schooling outcomes in the model and compare the model with the data.

Table 2 reports the Pareto shape parameter estimated in the data and in the model for 1983. The model accurately generates thicker tails for the non-SC/ST education distribution relative to SC/STs. The quantitative fit of the shape parameter is very close for non-SC/STs but somewhat less so for SC/STs. We interpret this as evidence that the model performs well in matching the observed schooling heterogeneity in 1983. This is important since schooling heterogeneity is the key for the economic heterogeneity in the model.

Having described the fit of the model to the data moments in 1983, we now examine its dynamic predictions for caste gaps. Table 2 also gives the labor and wage gaps across castes in the model and the data in 2012. The main takeaway from the Table is in the last row. In the data, the wage gap between non-SC/STs and SC/STs declined by 0.15/1.45 or 10.3 percent between 1983 and 2012. The corresponding reduction generated by the model is 7.5 percent. Thus, the baseline model can explain 72 percent of the observed decline in the percentage wage gap.

Underneath the success in reproducing the overall caste wage gap dynamics, the model also has qualitative and quantitative success in generating the observed dynamics of the caste gaps in both sectoral wages and employment shares. Thus, the agricultural wage gap marginally increased during 1983-2012 while the services wage gap decreased, both in the data and in the model. Correspondingly, the model reproduces the relatively unchanged agricultural labor share gap as well as the very sharp decline in the services labor share gap in the data. This last feature is particularly important since as the size of the change in the caste labor share gap in services was the largest amongst all the sectoral gaps. Given the average wage of the service sector is the highest among all sectors, the shrinking of labor share gap in the service sector plays the most important role in creating total wage convergence.

A key feature of the data is that there was a switch between the relative rank orders of the labor share gaps between manufacturing and services. While services had the largest caste gap in labor shares in 1983, by 2012 it was manufacturing that had the largest caste labor share gap. The model successfully reproduces this switch.

Table 2 also reports the change in the Pareto shape parameter for the schooling distribution of the two castes. Clearly, the model correctly matches the thickening tails of the schooling distribution for both castes, though with slightly more quantitative precision for non-SC/STs. We view this as evidence that sectoral productivity growth can account for a large part of the changes in the distribution of schooling outcomes in India since 1983.<sup>20</sup>

#### 4.1 Relative versus Absolute Convergence

The focal point of our paper is the convergence in relative wages between non-SC/STs and SC/STs. The focus on relative convergence is in keeping with the approach in the literature on inter-group inequalities which typically examines relative gaps between the groups of interest. Our focus on relative gaps is also consistent with the growth literature which looks at the relative income gaps across countries.

There is however, a parallel concern amongst some social scientists and policymakers about absolute inequality. Indeed, this is the reason why researchers sometimes use measures like the absolute Gini coefficient. Our model clearly has predictions for absolute wage convergence between

<sup>&</sup>lt;sup>20</sup>In the Appendix we also report the fit of the model in terms of aggregate prices and quantities. The noteworthy feature of this exercise is that the model is able to match the observed increase in the relative price of agriculture between 1983 and 2012. Most models of structural transformation have the opposite prediction for the relative price of agriculture.

castes. How do these predictions compare with the evidence on the behavior of absolute wage gaps between non-SC/STs and SC/STs during the period 1983-2012? Table 3 shows the change in the relative and absolute caste wage gaps in the data and in the model. We measure the relative caste wage gap at date t as  $w_{nt}/w_{st}$  and absolute caste wage gaps as  $w_{nt} - w_{st}$ . The table reports the percentage change between 1983 and 2012 in these two measures.

Table 3: Absolute versus Relative Convergence					
	Change: 1983-2012				
Variable	Data	Model			
Relative wage gap	-10.5	-7.5			
Absolute wage gap	71.3	96.0			
Note: The table reports changes in the relative					
and absolute wage gaps between non-SC/STs					
and SC/STs during 1983-2012					

TT 1 0 41 1 **D** 1 /·

As the table shows, the 10.5 percent decrease in the relative caste wage gap during 1983-2012 in the data was accompanied by a 71.3 percent increase in the absolute wage gap between the two groups during the period. Reassuringly, the model reproduces this feature of the data as well by predicting a 96 percent rise in the absolute wage gap.

We view the results in Table 3 as independent evidence in support of the model since it was not calibrated to target the absolute gaps either in 1983 or in 2012.

#### 4.2Misallocation and Welfare

The model induces talent misallocations due to caste-based schooling and sectoral entry costs. Consequently, equilibrium labor productivity in the model also depends on the education and sectoral sorting of workers. In the online appendix C we show that the growth induced re-sorting of workers can account for 44 percent, 37 percent and 11 percent of the overall sectoral labor productivity growth in Agriculture, Manufacturing and Services, respectively, during 1983-2012. Clearly, the productivity payoffs of declining misallocations were large.<sup>21</sup>

<sup>&</sup>lt;sup>21</sup>The online appendix D also shows that eliminating all caste-based distortions in the model would generate welfare gains of around 10% of per capita consumption.

### 5 Mechanism Underlying Convergence

The results above show that the model generates convergence in response to sectoral productivity shocks. What is the mechanism that generates this convergence? We investigate this issue by focusing on the two key margins that determine caste identities in the model. Recall that castes differ in the cost of schooling and the costs of accessing sectoral labor markets. These two costs induce a caste-specific sorting of agents into schooling and sectors which generates caste gaps in sectoral wages and employment. Changes in the caste wage gaps then are the result of differential changes in these caste specific schooling and labor market access costs which alter the schooling and sectoral choices by the two castes.

The two important cost parameters are the schooling cost  $\lambda$  and the entry cost parameter  $\phi$ . Both of these are denominated in terms of the final good, and are *constant*. Hence, growth reduces the *real* costs of access to schooling and sectoral labor markets. The decline in these costs change the schooling and sectoral employment decisions of agents. Consequently, if these costs change at different rates for the two castes, then the sectoral caste gaps in employment and wages would change since the two groups would respond differently in their schooling and employment decisions.

We examine the individual importance of the schooling and labor market frictions by conducting two experiments. First, we scale the entry cost scaling parameter  $\phi$  by the common growth factor. So, in this experiment, schooling costs become smaller due to growth but sectoral entry costs remain invariant. Second, we scale the schooling cost parameters  $\lambda_j$ , j = n, s by the common growth factor while leaving the entry cost parameter unscaled. Hence, in this case, the entry costs fall with growth but schooling costs remain invariant.<sup>22</sup> The results are reported in Table 4.

Table 4: Schooling and Sectoral Re-sorting						
		Scaling costs				
Variable	Data	Baseline	Scale entry cost	Scale schooling cost		
$\Delta s^a$	-1.25%	0.00%	0.00%	0.00%		
$\Delta s^m$	9.79%	50.35%	230.07%	36.36%		
$\Delta s^h$	-24.84%	-17.50%	-51.88%	5.00%		
$\Delta w^a$	3.85%	0.96%	0.00%	0.00%		
$\Delta w^m$	-5.00%	0.00%	10.83%	-0.01%		
$\Delta w^h$	-8.28%	-20.00%	-27.08%	0.00%		
$\Delta w$	-10.34%	-7.46%	-24.63%	5.22%		

The column "Scale entry cost" in Table 4 shows the percent changes in the predicted caste

<sup>&</sup>lt;sup>22</sup>In these experiments we scale the relevant costs using the common growth factor  $\frac{A_{2012}^{\theta}M_{2012}^{\eta}H_{2012}^{1-\theta-\eta}}{A_{1983}^{\theta}M_{1983}^{\eta}H_{1983}^{1-\theta-\eta}}$ 

employment and wage gaps in response to the measured productivity growth when entry costs are scaled but schooling cost remain unscaled. Correspondingly, the column "Scale schooling cost" shows the changes in the various caste gaps in response to productivity growth when schooling costs are scaled but sectoral entry cost are not. Relative to the baseline case, the results show that the fall in real schooling costs due to growth is key for generating the convergence in the overall caste wage gap since scaling entry costs alone *increases* the predicted convergence while scaling schooling costs alone induces a *divergence* in wages.

To understand these results, recall from equations 3.26 and 3.27 that the key determinants of the caste gaps are the ratios of ability thresholds which, in turn, are dependent on the relative costs of schooling and sectoral entry of the two castes. The calibrated schooling costs are proportionately greater for SC/STs in 1983. Hence, growth reduces schooling costs relatively faster for SC/STs. On the other hand, the calibrated sectoral entry costs are proportionately greater for non-SC/STs in 1983. Hence, growth reduces relatively faster for non-SC/STs.

Scaling entry costs alone prevents growth from reducing the relatively higher entry costs of non-SC/STs while the relatively higher schooling cost for SC/STs continues to decline with growth. Since SC/STs benefit more from this, the predicted wage convergence is greater in this case. On the other hand, scaling schooling costs alone while leaving entry costs unscaled switches the benefits of growth disproportionately towards non-SC/STS. Hence, the wage gap widens in this case.<sup>23</sup>

### 6 Evidence on Schooling Costs

The model has three features that are key for explaining both the caste wage gap as well as the decline in that gap over time: (a) real costs of schooling declined with growth; (b) schooling costs are higher for SC/STs relative to those for non-SC/STs; and (c) schooling costs declined relatively faster for SC/STS. We now examine the evidence on these features of the model.

### 6.1 Schooling costs and growth

Did the real costs of schooling in India decrease over the past three decades? We examine this issue directly using education price data and indirectly using teacher salary as well as education expenditure data.

The data on the Consumer Price Index (CPI) for education comes from the CPI for industrial

 $<sup>^{23}\</sup>mathrm{Scaling}$  both costs leaves all caste gaps unchanged since neither threshold changes.

workers which is collected by the Labor Bureau, Ministry of Labour and Employment of the Government of India. This data is at monthly frequency, covers 2006-2012 period, and is available across 85 centers located across India.<sup>24</sup> The data on teacher salaries and education expenditures is from the NSS household surveys and covers 1983-2012 period.

#### 6.1.1 Education price index and the CPI

We focus on the education and recreation index of the CPI for industrial workers as this is the highest level of disaggregation available.

We first compare the growth rates of education prices relative to the aggregate CPI across all districts. Columns 1 and 2 of Table 5 report the results. The education and recreation price index in India rose by 2.95 percent annually as compared to the 9.23 percent annual increase in the overall CPI during 2006-2012. Hence, the price of education relative to the price of the overall consumption basket declined during this period. This is exactly what the model demands.

Did real education costs decline faster for SC/STs? To answer this question, we exploit the geographic variation in SC/ST population shares across districts. We compute district-level population shares of SC/STs from the National Sample Survey of India for 2011-2012 round and use the threshold of 23.7 percent SC/ST population share (which is the mean SC/ST population share in our dataset) to split the districts into SC/ST and non-SC/ST dominant districts. We then map the 85 price centers from the Labor Bureau to these districts. This allows us to compare the growth of the education price index relative to the overall CPI in SC/ST dominated districts with that in non-SC/ST dominated districts. Column 3 of Table 5 shows that SC/ST dominant districts that are predominantly non-SC/ST. These results provide support to the basic mechanism in the model.

#### 6.1.2 Teacher salaries and growth

To supplement the evidence on education prices, we next compare the behavior of schooling costs relative to income growth by examining the relationship between average teacher salaries and per capita incomes across states in India during this period. This follows the approach of Banerjee and Duflo (2005) who examined a cross-country panel using teacher salaries as a proxy for schooling costs since teacher salaries tend to account for 80-90 percent of the cost of providing education.

<sup>&</sup>lt;sup>24</sup>The monthly CPI data release from the Ministry of Statistics and Programme Implementation (MOSPI) also contains indices on disaggregated categories including education at both the national and state levels. However this data is only available starting January 2011.

	CPI_edu	CPI_overall	$CPLedu/CPL_overall$
all districts	2.946	9.236	-6.290
	(0.068)	(0.020)	(0.069)
non-SC/STs districts			-6.067
			(0.094)
SC/STs districts			-6.551
			(0.095) - $0.485^{***}$
difference (SC/ST-non-SC/ST)			-0.485***
			(0.139)

Table 5: Annual growth rate of education and overall price indices in India, 2006-2012

Note: The Table reports average growth rates (in percent) of education and recreation CPI, overall CPI, and their ratio. Standard errors in parenthesis. \*\*\* p < 0.01

They found that a one percent increase in per capita GDP was associated with a rise in average teacher salaries by significantly less than one percent. Banerjee and Duflo (2005) concluded that the real cost of schooling declines with growth.

The teacher salary data for India comes from various rounds of the NSS. The NSS reports teachers under seven different occupation codes which we detail in the Appendix. We compute the average teacher salary across all the teaching occupations for each state in India for each round of the survey. We then regress the log of the average state teacher salary on log per capita state domestic product (SDP) using a panel of India states from 1983 to 2011-12. The estimated equation after controlling for state fixed effects is:<sup>25</sup>

$$\ln(Teacher\_salary) = 2.89^{***} + 0.22^{**}\ln(SDP\_pc), \quad R^2 = 0.22, \quad N = 155, \quad FE: Yes \quad (6.28)$$

The coefficient on log per capita SDP is significantly less than one indicating teacher salaries rise less than proportionately with per capita incomes. This result provides direct evidence for decreasing real costs of schooling (schooling costs in terms of final output) in India, which is the key mechanism driving convergence in the model.

#### 6.1.3 Education expenditures and growth

Our third piece of evidence in support of decreasing costs of education is based on household expenditures on education in India during 1983-2012 period. The data is from the consumption

<sup>&</sup>lt;sup>25</sup>The wage and SDP data are in constant 2004-05 rupees. \*\*\* indicates significance at the 0.1 percent level and \*\* indicates significance of the estimate at the 1 percent level.

expenditure schedule of the NSSO household surveys. Using this data we compute state-level averages of household education expenditures per household member for disaggregated education categories (books, tuition, tutoring, stationery, other), as well as for aggregate household education expenditure. We then regress the log of these state-level household education expenditures per household member on log per capita state domestic product. All variables are in real terms.<sup>26</sup> Table 6 reports the results. All regression coefficients are below 1 indicating that education costs rise less than proportionately with state income.<sup>27</sup> This evidence too indicates of decreasing education costs in India during this period.

Dependent variable: Log educational expenditure per household member on: (1)(2)(3)(4)(5)(6)total books tuition stationery other tutor 0.935\*\*\* 0.840\*\*\* 0.417\*\*\*  $0.633^{***}$ 0.428\*\*\*  $0.256^{***}$ lsdppc (0.176)(0.076)(0.179)(0.140)(0.100)(0.084) $\overline{N}$ 555555555555

Table 6: (Log) household education expenditures and state income, 1983-2012

Note: The Table reports marginal effects from a regression of log education expenditure for various categories on log state domestic product per capita (lsdppc); Standard errors in parentheses. \* p < 0.10, \*\* p < 0.05, \*\*\* p < 0.01

#### 6.2 Relative schooling costs of SC/STS

Our model generated caste wage gaps through a higher relative cost of schooling for SC/STs and caste wage convergence through a faster reduction in the schooling cost for SC/STs. We saw some evidence for the latter in the relative education price index movements of the two groups reported in Table 5. Assessing differences in education costs across SC/STs and non-SC/STs households is difficult since the levels of these costs are not directly observable.<sup>28</sup>

We address this issue by using a two pronged approach. We first compare the price **levels** of several education categories for SC/ST and non-SC/ST dominated districts in India. This is a direct approach to inferring relative education costs. We then examine the evidence on school

<sup>&</sup>lt;sup>26</sup>Consumption expenditures are deflated using state-level poverty lines that differ between rural and urban areas. State domestic product is in 2004-05 constant prices.

<sup>&</sup>lt;sup>27</sup>Unfortunately, we cannot estimate a similar regression of household education expenditures on household income since the latter is not available. When we used total household consumption expenditures to proxy for household income, we found that the results are similar to the state-level results.

<sup>&</sup>lt;sup>28</sup>A comparison of education consumption expenditures is one proxy, but it is problematic because expenditures can differ both due to their composition in the consumption baskets of the two social groups, and due to the differential prices that the two groups pay for education goods and services.

provisioning in SC/ST and non-SC/ST dominated districts in India during since 1991. This is an indirect approach to inferring the evolution of schooling costs for the two caste groups.

#### 6.2.1 Education prices across India

To examine differences in education costs across castes, we acquired detailed micro level data on prices of various education goods and services in India during 2006-2012 period across 85 centers from the Price Information System set up by the Department of Agriculture and Co-operation, Government of India. These data are used to construct education price index that we used in Section 6.1.1.

Here we focus on the monthly 7th and 9th grade tuition fees in different districts in India during 2006-2012 period.<sup>29</sup> To examine how levels of prices differ across SC/ST and non-SC/ST dominated districts we combine this price data with district-level population shares of SC/STs from the National Sample Survey of India for 2011-2012 round.

Table 7 reports average log tuition fees for the 7th and 9th grades during 2006-2012 period. The rows show average log fees for all districts, and separately for SC/ST and non-SC/St dominated districts. We see that the 7th grade tuition fees are significantly higher in SC/ST dominated districts though the 9th grade tuition fees are not significantly different.

To better exploit the geographic variation in our dataset, we regress the log of tuition fees on the SC/ST population shares across districts. The last row of Table 7 shows a significant positive relationship between them for both grade 7th and 9th tuition fees indicating that districts with higher SC/ST population also had higher tuition fees. These results suggest that SC/STs indeed faced higher costs of education, in line with our model mechanism.

#### 6.2.2 School provisioning

An alternative approach to determining schooling costs of the two caste groups is to examine the provisioning of schools in districts where each is dominant. We use Census data from India for 1991 and 2011 to examine the distribution of schools across towns and villages in India.<sup>30</sup> Our data comes from the SHRUG open data platform made available by the Development Data lab. Details about the data can be found in Asher et al. (2021).

<sup>&</sup>lt;sup>29</sup>We focus on these categories since they are the most homogeneous across centers and thus allow for a meaningful spatial comparison.

<sup>&</sup>lt;sup>30</sup>Digitized census data for India are available from 1991 onwards. This precludes the evaluation of school provisioning from 1981, which would have been closer to our household survey data start date of 1983.

#### HNATKOVSKA-HOU-LAHIRI: CASTE CONVERGENCE

	7th grade tuition fees	9th grade tuition fees
all districts	1.618	2.648
	(0.027)	(0.017)
non-SC/ST districts	1.322	2.650
	(0.036)	(0.024)
SC/ST districts	1.972	2.646
	(0.040)	(0.022)
difference (SC/ST-non-SC/ST)	$0.649^{***}$	-0.004
	(0.054)	(0.032)
regression of (log) tuition on SCST_population_share	2.736***	1.270***
· · · · · · ·	(0.267)	(0.129)

Table 7: Monthly tuition fees in India, 2006-2012

Note: The Table reports average (log) tuition fees for the 7th and 9th grades. Standard errors in parentheses. \*\*\* p < 0.01

Before presenting the evidence on school provisioning, it is important to reiterate that even though our model postulates schooling costs as being paid out of goods, there is an equivalence of that specification with ones where schooling costs are in terms of time. As argued in Section 3.7 the differences between the castes in the goods cost of education have a mapping to differences between the groups in the elasticity of human capital to schooling time. Increased provisioning of schools amounts to increasing the time elasticity of human capital which in turn has a mapping to decreasing costs of schooling.

Returning to the data on school provisioning, we are especially interested in two questions: (a) were there fewer schools in SC/ST dominated villages and towns relative to non-SC/ST dominated area? (b) did school provisioning increase faster during 1991-2011 in SC/ST dominated areas relative to non-SC/ST areas? If the answers to these two questions are affirmative then it provides indicative evidence that schooling costs were indeed higher for SC/STs but also declined at a faster rate than the schooling costs for non-SC/STs.

Table 8 reports the key statistics on school provisioning. We follow Bailwal and Paul (2021) and define a village or town to be dominated by caste k if the majority of the population in the village or town belongs to caste k where k = Non - SC/ST, SC, ST.

There are two takeaways from Table 8. First, the top panel of the Table shows that in 1991 non-SC/ST dominated geographic areas had a higher probability of having schools of all types. School provisioning in SC and ST villages and towns has improved over time but the gap with

	1991			2011		
Area Dominance:	$\mathbf{SC}$	ST	non-SC/ST	SC	ST	non-SC/ST
Probability of having school in the village or town						
Primary	0.56	0.55	0.71	0.76	0.83	0.84
Middle	0.09	0.11	0.24	0.31	0.33	0.49
Secondary	0.04	0.04	0.11	0.11	0.10	0.21
Fraction of people having school in the village or town						
Primary	90.1%	84.1%	91.4%	95.5%	96.1%	96.1%
Middle	45.9%	38.2%	52.9%	71.1%	59.6%	72.4%
Secondary	27.8%	22.6%	33.8%	41.9%	32.6%	46.7%
Obs	36,243	$53,\!446$	306,971	50,037	110,011	423,067

Table 8: Provisioning of Schools

non-SC/ST areas still remained in 2011.  $^{31}$ 

Second, the bottom panel of the Table reports the fraction of the different groups that live in areas that provide the various kinds of schools. As in the top panel, the results show that relative to non-SC/STs, a smaller fraction SCs and STs live in areas which have schools for all three categories of schools. Importantly, the gaps were much smaller relative to 1991 indicating a faster increase in school availability for SCs and STs as compared to non-SC/STs. <sup>32</sup>

We view these results as indicating that: (a) relative to non-SC/STs, schooling costs were greater for SC/STs in 1991; and (b) schooling costs declined relatively faster for SC/STs during 1991-2011. We interpret these findings as being supportive evidence for the schooling cost calibration for 1983 as well as their faster decline for SC/STs over time.<sup>33</sup>

An alternative interpretation of the schooling data above is that the faster increase in school provisioning in SC/ST dominated geographies after 1991 was due to public policy measures. Indeed, there were quite a few public policy initiatives since the 1990s that could have had this effect. The 73rd Amendment (1992) of the constitution provided for reservations for women and SC/STs in local governance. This could have improved local provisioning for education and resulted in differential

<sup>&</sup>lt;sup>31</sup>We estimate these probabilities by running logit regressions of a binary (1,0) variable indicating availability of school of type j = Primary, Middle, Secondary in the town or village on a constant and dummy variables for SC and ST domination of the area.

 $<sup>^{32}</sup>$ Note that this measure is not tied to whether a village or town is SC/ST dominated or not. Instead, it directly measures the share of people that have school access where they live.

<sup>&</sup>lt;sup>33</sup>In related work, Bailwal and Paul (2021) examine the distance to the nearest school from villages in India in 2001 and 2011 and find that (a) the distances to the nearest primary and middle schools are increasing in the village's SC and ST population shares; and (b) the positive correlation between distance to the nearest primary and middle schools and the SC/ST population share of the village declined between 2001 and 2011. While their sample period is different from our paper, nevertheless their finding (a) corroborates our calibration estimate of higher costs of schooling for SC/STs while their finding (b) provides support for a faster decrease in the cost of schooling for SC/STs during the sample.

outcomes in predominantly SC/ST areas. The District Primary Education Program (1993) and Sarva Shiksha Abhiyan (2000) could also have decreased the relative costs for SC/STs.

There is, however, considerable evidence that the spread of schooling after the 1990s was driven by a rapid expansion of private schools. Thus, Muralidharan and Kremer (2008) conducted a nationally representative survey in 2003 to document that: (a) 28 percent of rural Indians had access to a private school in their village; (b) most of the private schools were founded in the five years preceding 2003; (c) 40 percent of private school enrolment was in these newly founded schools; (d) the presence of private schools was *negatively* correlated with state and district per capita GDPs; and (e) the presence of a private school in a village was positively correlated with teacher absence rates in government schools in the village.

The results in Muralidharan and Kremer (2008) indicate that the growth of private schools was mainly a response to the absence of functioning public schools. We interpret this as evidence suggesting that there were important factors unrelated to public policy driving the expansion of school provisioning in India post-1991.<sup>34</sup>

### 7 Structural Transformation and Affirmative Action

Our approach has two features that require additional discussion. The first is the role of the structural transformation: how important is that for the predicted wage convergence? The second is the importance of affirmative action policies for our results.

#### 7.1 Caste Gaps and Structural Transformation

The baseline model has three mechanisms that induce structural transformation: (a) non-homothetic production technology; (b) differential sectoral productivity growth; and (c) unscaled schooling and sectoral entry costs. The first two are standard in many models of structural transformation. The last one is more specific to our model.

We examine the implications of structural transformation for the caste gaps by conducting a quantitative experiment where we remove all the ingredients in the model that induce structural transformation. Thus, we compare the baseline model to one where we impose a common sectoral

<sup>&</sup>lt;sup>34</sup>One could argue that post-1990s regulatory reform may have facilitated the growth of private schools. However, the major thrust of the criticisms of education policy changes during this period has been that they made the operation of private schools more onerous rather than less. For an in-depth review of the role of private schools in India, see Muralidharan (2019).

productivity growth (set at the aggregate growth rate), set  $\bar{y} = 0$ , and scale all the costs by making both  $\lambda_j$  and  $\gamma_j^k$ , k = m, h; j = n, s proportional to the growth rate of aggregate output.

Changes 1983-2012								
	Cast	e Gaps	Aggregate Sectoral Shares					
Variable	Baseline	No structural change	Variable	Baseline	No structural change			
$\Delta s^a$	0.15%	0.00%	$SL^a$	0.68 - 0.71	0.68 - 0.68			
$\Delta s^m$	50.23%	0.00%	$SL^m$	0.19 - 0.12	0.19 - 0.19			
$\Delta s^h$	-17.41%	0.00%	$SL^h$	0.13 - 0.17	0.13 - 0.13			
$\Delta w^a$	0.26%	0.00%	$SY^a$	0.46 - 0.37	0.46 - 0.46			
$\Delta w^m$	0.38%	0.00%	$SY^m$	0.15 - 0.12	0.15 - 0.15			
$\Delta w^h$	-19.96%	0.00%	$SY^h$	0.39 - 0.51	0.39 - 0.39			
$\Delta w$	-7.53%	0.00%						

Table 9:	Role	of	Structural	Transformation

Notes: The left panel of the table gives changes in the caste gaps in sectoral employment and wages between 1983 and 2012 in the baseline case and in the case of no structural change with  $\bar{y} = 0$ , common sectoral growth rate, and scaled schooling and sectoral entry costs. The right panel gives the corresponding changes under the baseline case and in the case with no structural change.  $SL^k$  denotes the employment share of sector k = a, m, h.  $SY^k$  denotes the output share of sector k = a, m, h.

The main takeaway from the numbers in Table 9 under the columns for  $\bar{y} = 0$  is that without the conditions that generate structural transformation, productivity changes have no impact on the caste employment and wage gaps. Intuitively, when all sectors grow at a common rate, ability thresholds for the two castes are unaffected by productivity growth since the rewards from switching sectors change at the same rate as the costs of schooling and accessing sectors.

### 7.2 Affirmative Action Policies

The Indian constitution mandates reservations of seats in public institutions of tertiary education, in public sector employment and in political representation for SC/STs. How important were these reservations for the observed caste convergence between 1983 and 2012?

Recall that our calibration of the model for 1983 dictated lower fixed costs of accessing manufacturing and service sector employment for SC/STs. We view these lower sectoral entry costs of SC/STs as the proxy for reservations in the model. To examine the importance of reservations, we conducting three counterfactual simulations: (a)  $\frac{\gamma_n^m}{\gamma_s^m} = 1$ ; (b)  $\frac{\gamma_n^h}{\gamma_s^h} = 1$ ; and (c)  $\frac{\gamma_n^m}{\gamma_s^m} = \frac{\gamma_n^h}{\gamma_s^h} = 1$ . In these experiments we leave  $\gamma_n^m$  and  $\gamma_n^h$  at their baseline levels. In other words, we raise the fixed cost component of sectoral entry costs for SC/STs to non-SC/STs levels in each sector thereby *eliminating*  the advantage of reservations for SC/STs. All other baseline parameters remain unchanged.

1983 2012  $\gamma^h$  $\gamma^{\overline{h}}$ Variable Data Baseline  $\gamma^m$ both Data Baseline  $\gamma^m$ both  $\Delta s^a$ 0.800.850.840.850.840.790.850.840.850.84 $\Delta s^m$ 2.152.541.431.431.540.790.841.570.770.84 $\Delta s^h$ 1.611.601.5893.3782.781.211.331.313.903.84 $\Delta w^a$ 1.081.041.041.011.041.011.051.011.051.01 $\Delta w^m$ 1.201.201.181.011.001.141.201.181.021.00 $\Delta w^h$ 1.451.441.451.261.261.331.161.161.021.02 $\Delta w$ 1.451.341.311.621.581.301.241.221.331.31Notes: For  $j = a, m, h, \Delta s^{j}$  is the ratio of the fraction of all non-SC/STs working in

Table 10: Role of Affirmative Action

Notes: For  $j = a, m, h, \Delta s^j$  is the ratio of the fraction of all non-SC/STs working in sector j to the fraction of all SC/STs working in sector j;  $\Delta w^j$  is the ratio of the mean non-SC/ST to mean SC/ST wage in sector j;  $\Delta w$  is the ratio of the mean non-SC/ST to mean SC/ST wage.

The left panel of Table 10 shows the effects of equalizing sectoral entry costs in 1983 while the right panel shows the corresponding effects in 2012. Comparing the "both" and "Baseline" columns in the Table reveals that when both sectoral entry costs are equalized, the overall wage gap in 1983 rises to 1.58 from the baseline level of 1.34 while for 2012 the gap rises to 1.31 from the baseline of 1.24. Clearly, reservations reduced the level of the wage gap at all dates. However, since the *level* of the gap rises at both dates, removing reservations has a muted effect on its *dynamics*.

We view these results as indicating that affirmative action policies may have affected the level of the wage gaps but not their dynamics during 1983-2012.

## 8 Conclusion

The paper has examined the role of growth in accounting for the observed convergence in the education, sectoral employment and wages of scheduled castes and tribes (SC/STs) in India toward the levels of non-SC/STs during 1983-2012.

We formalized a tractable multi-sector, heterogenous agent model where all individuals draw their innate ability from the same ability distribution but their costs of acquiring schooling and accessing sectoral labor markets depend on their caste. We examined the dynamic effects of exogenous productivity growth on caste gaps in this environment with caste-based talent misallocations. Our quantitative experiments on the model suggest that exogenous sectoral productivity growth can account for 72 percent of the observed wage convergence between SC/STs and non-SC/STs during 1983-2012.

The main mechanism driving the caste convergence in the model is SC/STs increasing their relative education levels in response to decreasing real costs of schooling. We provided independent evidence in support of this mechanism using India-wide data on education prices, teacher salaries and school provisioning. In particular, we showed that: (a) the education CPI grew slower than the overall CPI so that the relative price of education in India declined; (b) the price of education as measured by tuition fees declined faster in SC/ST dominated districts; (c) the cost of schooling proxied by teacher salaries declined with growth in India; and (d) villages and towns dominated by SC/STs saw a faster increase in provisioning of schools during 1991-2011.

The findings of the paper indicate that growth during 1983-2012 may have succeeded in breaking down millenia of the socio-economic disparities induced by caste-based distortions. This suggests that growth focused policies may be more potent than group-based redistribution policies for reducing inter-group inequalities.

A related issue to caste gaps is gender gaps. This has attracted a lot of attention in India over recent years particularly due to large gender gaps in labor force participation rates. We believe our approach can be adapted to address that issue as well.

## References

- Acemoglu, D. and V. Guerrieri (2008, 06). Capital deepening and nonbalanced economic growth. Journal of Political Economy 116(3), 467–498.
- Asher, S., T. Lunt, R. Matsuura, and P. Novosad (2021). Development Research at High Geographic Resolution: An Analysis of Night Lights, Firms, and Poverty in India using the SHRUG Open Data Platform. *The World Bank Economic Review*.
- Bailwal, N. and S. Paul (2021). Caste discrimination in provision of public schools in rural india. Journal of Development Studies 57(11), 1830–1851.
- Banerjee, A. and E. Duflo (2005). Growth theory through the lens of development economics. InP. Aghion and S. Durlauf (Eds.), *Handbook of Economic Growth* (1 ed.), Volume 1, Part A,Chapter 07, pp. 473–552. Elsevier.

- Banerjee, A. and K. Munshi (2004). How efficiently is capital allocated? evidence from the knitted garment industry in tirupur. *Review of Economic Studies* 71(1), 19–42.
- Banerjee, B. and J. Knight (1985). Caste discrimination in the indian urban labour market. *Journal* of Development Economics 17(3), 277–307.
- Bertrand, M., R. Hanna, and S. Mullainathan (2010). Affirmative action in education: Evidence from engineering college admissions in india. *Journal of Public Economics* 94(1-2), 16–29.
- Bhattacharjee, S., V. Hnatkovska, and A. Lahiri (2015). The evolution of gender gaps in india. In S. Shah, A. Panagariya, and S. Gokarn (Eds.), *India Policy Forum 2014-15*, Volume 11. Sage Publications, Brookings and NCAER.
- Borooah, V. K. (2005, 08). Caste, inequality, and poverty in india. Review of Development Economics 9(3), 399–414.
- DiNardo, J., N. M. Fortin, and T. Lemieux (1996, September). Labor market institutions and the distribution of wages, 1973-1992: A semiparametric approach. *Econometrica* 64(5), 1001–44.
- Herrendorf, B., R. Rogerson, and A. Valentinyi (2014). Growth and Structural Transformation.
  In P. Aghion and S. Durlauf (Eds.), *Handbook of Economic Growth*, Volume 2 of *Handbook of Economic Growth*, Chapter 6, pp. 855–941. Elsevier.
- Hnatkovska, V., C. Hou, and A. Lahiri (2024). Urbanization, structural transformation and ruralurban disparities in china and india. Working paper, University of British Columbia.
- Hnatkovska, V., A. Lahiri, and S. Paul (2012, April). Castes and labor mobility. American Economic Journal: Applied Economics 4(2), 274–307.
- Hnatkovska, V., A. Lahiri, and S. Paul (2013, Spring). Breaking the caste barrier: Intergenerational mobility in india. Journal of Human Resources 48(2), 435–473.
- Hsieh, C., E. Hurst, C. I. Jones, and P. J. Klenow (2019, September). The Allocation of Talent and U.S. Economic Growth. *Econometrica* 87(5), 1439–1474.
- Ito, T. (2009). Caste discrimination and transaction costs in the labor market: Evidence from rural north india. *Journal of Development Economics* 88(2), 292–300.

- Kongsamut, P., S. Rebelo, and D. Xie (2001). Beyond balanced growth. Review of Economic Studies 68(4), 869–882.
- Munshi, K. (2019, December). Caste and the indian economy. Journal of Economic Literature 57(4), 781–834.
- Munshi, K. and M. Rosenzweig (2006). Traditional institutions meet the modern world: Caste, gender, and schooling choice in a globalizing economy. *American Economic Review* 96(4), 1225–1252.
- Munshi, K. and M. Rosenzweig (2016, January). Networks and Misallocation: Insurance, Migration, and the Rural-Urban Wage Gap. American Economic Review 106(1), 46–98.
- Muralidharan, K. (2019). The State and the Market in Education Provision: Evidence and the Way Ahead. SIPA Working Papers 2019-06, Columbia—SIPA.
- Muralidharan, K. and M. Kremer (2008). Public and Private Schools in Rural India. In P. P. . R. Chakrabarti (Ed.), *School Choice International*. MIT.
- Ngai, L. R. and C. A. Pissarides (2007, March). Structural change in a multisector model of growth. *American Economic Review* 97(1), 429–443.

# A Appendix

### A.1 Data

Our primary data source is the National Sample Survey (NSS) employment-unemployment household surveys from 1983 to 2011-12. We consider individuals between the ages 16-65 belonging to male-headed households who were not enrolled full time in any educational degree or diploma. The sample is restricted to those individuals who provided their 4-digit industry of employment information as well as their education information.<sup>35</sup>

Our focus is on full-time working individuals who are defined as those that worked at least 2.5 days per week. This selection leaves us with a working sample of around 165,000-182,000 individuals, depending on the survey round. The wage data is more limited. This is primarily due to the prevalence of self-employed individuals in rural India who do not report wage income. This limits the sub-sample with wage data to about 48,000 individuals on average across rounds.

In the text we group the reported industry codes into three broad industry categories: Ind 1 refers to Agriculture, Hunting, Forestry and Fishing; Ind 2 collects Manufacturing and Mining and Quarrying; Ind 3 refers to all Service industries. These groupings are detailed in Table 11.

Industry code	Industry description	Group
А	Agriculture, Hunting and Forestry	Ind 1
В	Fishing	Ind 1
С	Mining and Quarrying	Ind 2
D	Manufacturing	Ind 2
E	Electricity, Gas and Water Supply	Ind 3
F	Construction	Ind 3
G	Wholesale and Retail Trade; Repair of Motor Vehicles,	Ind 3
	motorcycles and personal and household goods	
Н	Hotels and Restaurants	Ind 3
Ι	Transport, Storage and Communications	Ind 3
J	Financial Intermediation	Ind 3
Κ	Real Estate, Renting and Business Activities	Ind 3
L	Public Administration and Defence; Compulsory Social Security	Ind 3
Μ	Education	Ind 3
Ν	Health and Social Work	Ind 3
0	Other Community, Social and Personal Service Activities	Ind 3
Р	Private Households with Employed Persons	Ind 3
Q	Extra Territorial Organizations and Bodies	Ind 3

Table 11: Industry categories

<sup>35</sup>We also consider a narrower sample in which we restrict the sample to only males and find that our results remain robust.

### A.2 Sectoral education levels

Figure 6 shows that there is clear rank-order in the average years of education of workers in the three sectors in our sample. Specifically, for all the sample rounds, the average years of education is the highest for service sector workers followed by manufacturing workers which is followed by agricultural workers.

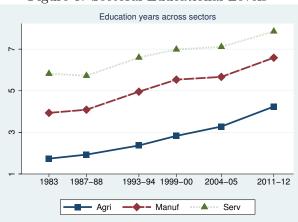


Figure 6: Sectoral Educational Levels

### A.3 Structural transformation

Figure 7 shows that 1983-2012 witnessed a gradual contraction in the agricultural sector along with an expansion of the service sector.

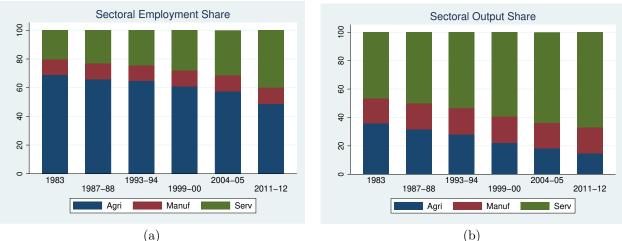


Figure 7: Industry distribution

Notes: Panel (a) gives the industrial distribution of workers for different NSS rounds. Panel (b) presents distribution of output (measured in constant 1980-81 prices) across three industry categories.

### A.4 Teacher occupation data

The NSSO data classifies the teaching profession under 3 primary NCO codes and 4 teaching associate professional codes. The details are provided in the table below.

	Table 12: Teacher occupation categories
NCO Code	Description
231	College University and High School education teaching professionals
232	Secondary education teaching professional
233	Other teaching professional
331	Middle and primary teaching associate professional
332	Pre-primary teaching associate professional
333	Special education teaching associate professional
334	Other teaching associate professional

# Table 12: Teacher occupation categories

### A.5 Proofs of Lemmas 3.1 and 3.2

To ease notation, throughout this section we will use the definition:

$$\Psi_j \equiv (1 - \chi) \left(\frac{\chi}{\lambda_j}\right)^{\frac{\chi}{1 - \chi}}$$

**Lemma 3.1** All individuals  $i \in caste \ j = n, s$  with ability  $a_{ij}$  prefer employment in sector-m to employment in sector-a if  $a_{ij} \ge \hat{a}_j^m$ ; employment in sector-h to sector-a if  $a_{ij} \ge \hat{a}_j^h$ ; and employment in sector-h to sector-m if  $a_{ij} \ge \tilde{a}_j^h$ .

*Proof.* The agent will choose the sector that gives the highest  $c_{ij}^k$ . It is easy to see that the agent prefers sector a to m if and only if  $c_{ij}^a \ge c_{ij}^m$ . Similarly, she prefers a to h iff  $c_{ij}^a \ge c_{ij}^h$  and m to h if and only if  $c_{ij}^m \ge c_{ij}^h$  where  $c_{ij}^a, c_{ij}^m$  and  $c_{ij}^h$  are given by equations 3.10, 3.11 and 3.12, respectively. We can rewrite these three conditions and define:

$$z_{j}^{m}(a_{ij}) \equiv \frac{\phi \gamma_{j}^{m}}{a_{ij}^{\frac{1}{1-\chi}}} \ge \Psi_{j} (p^{m}M + \phi \alpha)^{\frac{1}{1-\chi}} - \Psi_{j} (p^{a}A)^{\frac{1}{1-\chi}}$$
(A.29)

$$z_{j}^{h}(a_{ij}) \equiv \frac{\phi \gamma_{j}^{h}}{a_{ij}^{\frac{1}{1-\chi}}} \ge \Psi_{j} (p^{h}H + \phi \alpha)^{\frac{1}{1-\chi}} - \Psi_{j} (p^{a}A)^{\frac{1}{1-\chi}}$$
(A.30)

$$z_{j}^{h}(a_{ij}) - z_{j}^{m}(a_{ij}) \equiv \frac{\phi(\gamma_{j}^{h} - \gamma_{j}^{m})}{a_{ij}^{\frac{1}{1-\chi}}} \ge \Psi_{j}(p^{h}H + \phi\alpha)^{\frac{1}{1-\chi}} - \Psi_{j}(p^{m}M + \phi\alpha)^{\frac{1}{1-\chi}}$$
(A.31)

With  $0 < \chi < 1$ ,  $\phi$ ,  $\gamma_j^k > 0$  and Assumption 2, it is obvious that  $z_j^m(a_{ij})$ ,  $z_j^h(a_{ij})$  and  $z_j^h(a_{ij}) - z_j^m(a_{ij})$ are strictly decreasing in  $a_{ij}$ . Since  $p^h H + \phi \alpha > p^m M + \phi \alpha > p^a A$  (Assumption 3), we have:

$$\begin{cases} c_{ij}^a \le c_{ij}^m & \text{iff } a_{ij} \ge \hat{a}_j^m \\ c_{ij}^a \le c_{ij}^h & \text{iff } a_{ij} \ge \hat{a}_j^h \\ c_{ij}^m \le c_{ij}^h & \text{iff } a_{ij} \ge \tilde{a}_j^h \end{cases}$$

Lemma 3.2: The rank order of the three ability thresholds are

$$\begin{split} \tilde{a}_j^h < \hat{a}_j^h < \hat{a}_j^m & \text{if} \quad \hat{a}_j^h = \min[\hat{a}_j^m, \hat{a}_j^h] \\ \tilde{a}_j^h > \hat{a}_j^h > \hat{a}_j^m & \text{if} \quad \hat{a}_j^h = \max[\hat{a}_j^m, \hat{a}_j^h] \end{split}$$

*Proof.* Consider first the case  $\hat{a}_j^h < \hat{a}_j^m$ . In this case, suppose  $\tilde{a}_j^h > \hat{a}_j^h$ . Using the definitions of  $\hat{a}_j^h$  and  $\tilde{a}_j^h$  from equations 3.14 and 3.15 above,  $\tilde{a}_j^h > \hat{a}_j^h$  can be rewritten as

$$\left[\frac{\phi\gamma^{h}}{\left(1-\chi\right)\left(\frac{\chi}{\lambda_{j}}\right)^{\frac{\chi}{1-\chi}}\left\{\left(p^{h}H+\phi\alpha\right)^{\frac{1}{1-\chi}}-\left(p^{a}A\right)^{\frac{1}{1-\chi}}\right\}}\right]^{1-\chi}>\left[\frac{\phi\gamma^{m}}{\left(1-\chi\right)\left(\frac{\chi}{\lambda_{j}}\right)^{\frac{\chi}{1-\chi}}\left\{\left(p^{m}M+\phi\alpha\right)^{\frac{1}{1-\chi}}-\left(p^{a}A\right)^{\frac{1}{1-\chi}}\right\}}\right]^{1-\chi}$$

But this implies that  $\hat{a}_j^h > \hat{a}_j^m$  which is a contradiction. Hence, if  $\hat{a}_j^h < \hat{a}_j^m$  then  $\tilde{a}_j^h < \hat{a}_j^h < \hat{a}_j^m$ .

The other case  $\hat{a}_j^h > \hat{e}_j^m$  but  $\hat{a}_j^h > \tilde{a}_j^h$  leads to a contradiction by a similar logic. Hence, if  $\hat{a}_j^h > \hat{a}_j^m$  then  $\tilde{a}_j^h > \hat{a}_j^h > \hat{a}_j^m$ .

#### A.6 Sectoral prices and quantities

Table 13 shows the percent change in sectoral prices and quantities in the data and their model counterparts during the period 1983-2012.

Two features of the results in Table 13 are noteworthy. First, the model does well in matching the dynamics of the relative prices and quantities of agriculture and services. The predicted dynamics of the agricultural relative price is particularly important in this context. As the Table shows, the relative price of agriculture actually rose during 1983-2012 in India. The model matches this fact. We view this as a particular strength of the model since standard models of

### HNATKOVSKA-HOU-LAHIRI: CASTE CONVERGENCE

		Percent chang	ge 1983-2012			
VARIABLE	Notation	Data	Model			
Relative price Agri	$p^a$	+20.6%	+21.3%			
Relative price Manuf	$p^m$	-8.5%	+21.0%			
Relative price Serv	$p^h$	-6.2%	-26.0%			
Output Share Agri	$y^a$	-75.0%	-19.6%			
Output Share Manuf	$y^m$	+28.6%	-20.0%			
Output Share Serv	$y^h$	+126.7%	+30.8%			
Notes: The table reports the percent changes of sectoral						
prices and quantities in the data and the model.						

Table 13: Sectoral Prices and Quantities

=

=

structural transformation which generate a declining share of agriculture over time have difficulty in simultaneously generating a rising agricultural relative price.<sup>36</sup>

Second, the model encounters difficulties in reproducing the dynamics of the manufacturing sector, both in quantities and prices. It predicts an increase in the relative price of manufacturing and a decrease in its output share. Both are counterfactual. This aspect of the model is similar to its relative underperformance in matching the dynamics of the caste gaps in manufacturing.

<sup>&</sup>lt;sup>36</sup>Standard models of structural transformation based on non-homothetic demand for the agricultural good predict that the relative price of agriculture declines in response to productivity growth since its demand rises less than proportionately with income. Models that generate structural transformation through inelastic elasticity of substitution across sectors predict that resources flow towards the slower growing non-agricultural sectors as their relative prices rise (see Ngai and Pissarides (2007)). But this is counterfactual in the Indian data during 1983-2012 when agriculture was the slowest growing sector.

# **Online Appendix for "Convergence of Castes"**

Viktoria Hnatkovska

Chenyu(Sev) Hou

University of British Columbia

Simon Fraser University

Amartya Lahiri University of British Columbia December 2, 2024

# Appendices

# A Equivalence between goods and time cost for education

We examine three versions of a simple one-sector model where schooling costs can be paid for with either **goods** or **time** or **both goods and time** We show that there is an equivalence between these versions with all the versions sharing the feature that human capital, income and consumption increasing with productivity of the final goods sector.

We work with a simplified version of the model with only one sector. Considering the simple model eases our exposition and is without loss of generality, as in our baseline model, the schooling choices are conditional on sectoral choice. The model structure is close to our baseline model: production technology is linear:  $y_i = Ae_in_i$ , where  $e_i$  is human capital,  $n_i$  is labor, and A is productivity. Agents have an endowment of one unit of time, which can be allocated to either school or work, or both, depending on the precise productivity of time in these activities. Each individual i with an innate ability endowment  $a_i$ . Each agent makes decisions to maximize  $u(c_i - \bar{c})$ 

<sup>\*</sup>We would like to thank Tasso Adamopoulos, Paul Beaudry, Satyajit Chatterjee, Rana Hasan, Chang-Tai Hsieh, Ashok Kotwal, Devashish Mitra, Dilip Mookherjee, B. Ravikumar, Richard Rogerson, and seminar participants at the CMSG-Montreal, IGC conference (Delhi), FRB St Louis-LAEF-Human Capital conference in Santa Barbara, NBER Summer Institute, IIT-Delhi, IIT-Kanpur, UCSD, Peking University, Pennsylvania State University, FRB Philadelphia, University of Maryland and USC for helpful comments and discussions. Thanks to Sudipta Ghosh for providing research assistance. We also thank the IGC for providing funding to support this research.

where  $\bar{c}$  denotes minimum consumption.

### A.1 Baseline model: Goods cost of education

**Human Capital Accumulation:** Human capital is a function of schooling  $q_i$  chosen by the individual:

$$e_i = a_i q_i^{\chi}$$

Choosing  $q_i$  units of schooling incurs a good cost:  $\lambda q_i$ .

**Consumption and Production:** The individual faces the budget constraint:

$$c_i = y_i - \lambda q_i = Aa_i q_i^{\chi} - \lambda q_i$$

To maximize her welfare given by  $u(c_i - \bar{c})$ , the agent chooses schooling  $q_i$ . The optimal solutions for this problem are:

$$q_i^* = \left(\frac{\chi}{\lambda}Aa_i\right)^{\frac{1}{1-\chi}}$$

$$e_i^* = A^{\frac{\chi}{1-\chi}}a_i^{\frac{1}{1-\chi}}\left(\frac{\chi}{\lambda}\right)^{\frac{\chi}{1-\chi}}$$

$$c_i^* = (1-\chi)\left(Aa_i\right)^{\frac{1}{1-\chi}}\left(\frac{\chi}{\lambda}\right)^{\frac{\chi}{1-\chi}}$$

These results are consistent with our baseline model. In particular, schooling, human capital, and production are all increasing in A and  $a_i$  but decreasing in  $\lambda$ .

### A.2 Human Capital with both goods and time cost

We now turn to a specification in which schooling requires the input of both goods and time.

**Human Capital Accumulation:** We follow Hsieh et al. (2019) by modelling the human capital technology as :

$$e_i = a_i \mu (1 - n_i)^\theta g_i^\eta$$

where  $\theta$  captures the return to time investments of human capital,  $\eta$  is the return to goods investment of human capital,  $\mu$  is the production technology to transform goods and time into human capital. The cost of time is the *opportunity cost* of decreasing working time  $n_i$ , the cost of goods investment is the *direct cost* in terms of consumption goods,  $g_i$ .

Consumption and Production: Household consumption is output net of the goods cost of schooling. Since  $y_i = a_i e_i$ , consumption is:

$$c_i = y_i - g_i = Aa_i\mu(1 - n_i)^{\theta}g_i^{\eta}n_i - g_i$$

The optimal allocation of time  $n_i$  and goods investment in schooling  $g_i$  are:

$$\hat{n}_i = \frac{1}{1+\theta} \hat{g}_i = \eta y_i$$

We should note that the time spent on schooling in this version is constant across individuals but the goods investment in schooling, which is proportional to individual output, is different. These results are in line with those in Hsieh et al. (2019).

Substituting these solutions into the production functions for human capital and the final good yields the equilibrium solutions:

$$\hat{e}_{i} = A^{\frac{\eta}{1-\eta}} \left[ a_{i}\mu \left(\frac{\theta}{1+\theta}\right)^{\theta} \right]^{\frac{1}{1-\eta}} \left(\frac{\eta}{1+\theta}\right)^{\frac{\eta}{1-\eta}}$$

$$\hat{g}_{i} = \left[ \eta A a_{i}\mu \left(\frac{\theta}{1+\theta}\right)^{\theta} \left(\frac{1}{1+\theta}\right) \right]^{\frac{1}{1-\eta}}$$

$$\hat{y}_{i} = \left[ \eta^{\eta} A a_{i}\mu \left(\frac{\theta}{1+\theta}\right)^{\theta} \left(\frac{1}{1+\theta}\right) \right]^{\frac{1}{1-\eta}}$$

$$\hat{c}_{i} = (1-\eta) \left[ \eta^{\eta} A a_{i}\mu \left(\frac{\theta}{1+\theta}\right)^{\theta} \left(\frac{1}{1+\theta}\right) \right]^{\frac{1}{1-\eta}}$$

Now consider the following parameter specification:

$$\chi = \eta \tag{A.32}$$

$$\frac{1}{\lambda} = \left[ \mu \left( \frac{\theta}{1+\theta} \right)^{\theta} \left( \frac{1}{1+\theta} \right) \right]^{\frac{1}{\eta}}$$
(A.33)

It is easy to check that under this parameter configuration

$$\hat{c}_i = c_i^*$$
$$\hat{e}_i = (1+\theta)e_i^*$$

Hence, consumption for each individual of ability  $a_i$  is the same in both models while human capital in the two versions differs by a constant scalar that is unrelated to either ability or aggregate productivity. Similarly, output in the two version are scalar multiples of each other with the scalar factor being related to  $\theta$  and unrelated to either individual ability  $a_i$  or aggregate productivity A.

Importantly, equation (A.33) provides a mapping between the goods cost of education,  $\lambda$ , in the baseline model and the time elasticity of human capital in the time cost version,  $\theta$ , which renders the two versions isomorphic to each other. Note that this mapping describes an inverse relationship between  $\lambda$  and  $\theta$ .

### A.3 Human Capital with only time cost

Lastly, we consider a model where human capital is accumulated only through time investment into schooling but where individuals choose the allocation of their time between school and leisure.

**Human Capital Accumulation:** The human capital is a function of ability  $a_i$  and time spent on schooling  $l_i$ . The human capital accumulation technology is:

$$e_i = a_i l_i^{\theta}$$

with  $\theta > 0$ .  $l_i$  is time invested when the individual is at school age. After accumulating  $e_i$ , she can earn a fair wage of production depending on her human capital:

$$y_i = Ae_i = Aa_i l_i^{\theta}$$

### Household's maximization:

$$\max_{c_i, l_i} \left\{ \frac{c_i^{1-\sigma}}{1-\sigma} - \frac{l_i^{1+\kappa}}{1+\kappa} \right\}$$

This is subject to the budget constraint:

 $c_i = y_i = Aa_i l_i^{\theta}$ 

The cost of time spent on schooling is the disutility of foregone leisure (as a child) instead of the opportunity cost of losing income. Hence, this version excludes environments that resemble child labor.

Solving the optimization problem gives the optimal time investment in schooling:

$$\hat{l}_i^* = \theta^{\frac{1}{\kappa+1-(1-\sigma)\theta}} (Aa_i)^{\frac{1-\sigma}{\kappa+1-(1-\sigma)\theta}}$$

Note that for  $\hat{l}_i^*$  to be increasing in productivity A and ability  $a_i$ , we need:

$$\theta < \frac{1+\kappa}{1-\sigma}$$

The optimal consumption is then:

$$\hat{c}_i^* = A\hat{e}_i^*$$

Recall that in the baseline model with only goods cost for schooling, optimal consumption was  $c_i^* = (1 - \chi)y_i^* = (1 - \chi)Ae_i^*$ . It is obvious that  $\hat{e}_i^* = (1 - \chi)e_i^*$  is equivalent to  $\hat{c}_i^* = c_i^*$ .

Substituting the solution for  $\hat{l}^*$  into the production function gives optimal consumption:

$$\hat{c}_i^* = Aa_i \hat{l}_i^{*\theta} = \left(Aa_i \theta^{\frac{\theta}{1+\kappa}}\right)^{\frac{1+\kappa}{1+\kappa-(1-\sigma)\theta}}$$

Note that the condition  $\theta < \frac{1+\kappa}{1-\sigma}$  guarantees that consumption and human capital will both be increasing in A and  $a_i$ .

Equivalence between goods and time investment in education: For  $\hat{c}_i^* = c_i^*$  we need:

$$\begin{cases} \frac{1}{1-\chi} &= \frac{1+\kappa}{1+\kappa-(1-\sigma)\theta} \\ (1-\chi) \left(\frac{\chi}{\lambda}\right)^{\frac{\chi}{1-\chi}} &= \theta^{\frac{\theta}{1+\kappa-(1-\sigma)\theta}} \end{cases}$$

For each value of  $\sigma$ ,  $\kappa$  and  $\lambda$ , consider:

$$\frac{(1-\sigma)\theta}{1+\kappa} = \chi$$

So the first equation holds. Note that in our baseline model,  $0 < \chi < 1$  and in the time model  $\theta > 0$ , so these conditions guarantee  $\theta < \frac{1+\kappa}{1-\sigma}$ . Rearrange the second equation:

$$[\lambda^{-1}\chi(1-\chi)^{1-\chi}]^{\frac{1}{1-\chi}} = \left[\theta^{\frac{\theta}{1+\kappa}}\right]^{\frac{1}{1-\chi}}$$

So the above conditions boil down to:

$$\frac{\chi}{1-\sigma} = \frac{\theta}{1+\kappa} \tag{A.34}$$

$$\theta^{\frac{\theta}{1+\kappa}} = \left(\frac{\lambda}{\chi}\right) (1-\chi)^{1-\chi}$$
(A.35)

There are three key properties of this model that relate to our baseline model:

- 1. For the parameters in our baseline,  $0 < \chi < 1$ , the time invested in education, human capital, and consumption are all increasing in productivity A and ability  $a_i$ .
- 2. For any given values of the parameters  $\sigma$ ,  $\chi$ , and  $\lambda$  in our baseline model, there exist values for  $\kappa$  and  $\theta$  in the time investment model, such that the optimal human capital and consumption levels chosen by an individual with ability  $a_i$  are *identical* in the baseline (goods cost) and time cost models.
- 3. The equivalence between the time cost and goods cost versions arises from the fact that the elasticity of human capital with respect to schooling time (θ) has an inverse mapping to the goods cost of education (λ) which is jointly defined by equations (A.34) and (A.35). As in the second version with both goods and time costs of schooling described above, this version too implies that a lower time elasticity of human capital implies greater foregone goods production. Hence, in our example, the model with time costs of schooling can be rewritten as a model with goods costs of education with a suitable specification of the goods cost parameter in terms of the time elasticity parameter.

## **B** Growth, Education and Entry Costs

In our model SC/STs and non-SC/STs differ along two margins: the cost of education and the costs of sectoral labor market entry. Our baseline calibration strategy was to calibrate these cost parameters to target the 1983 sectoral caste gaps. We then evaluated the role of growth during 1983-

impact these costs but only indirectly through its effect on the costs relative to the final good.

2012 in generating caste convergence by allowing sectoral productivities to change while keeping the calibrated caste-specific cost parameters fixed at their 1983 levels. In our model growth did

One concern with this strategy is that there could have been changes in policy or social conventions during 1983-2012 that might have changed the caste-specific education and sectoral entry costs directly. For example, policy initiatives such as Operation Blackboard (1987) and the Right to Education Act (2002) were aimed directly at deepening education pathways for the populace. In as much as these policies aided SC/STs more than non-SC/STs, they may have directly lowered the costs of education for SCSTs relative to non-SC/STs. Extension of job reservation policies to Other Backward Castes (1992) could have directly reduced the relative sectoral entry costs for non-SC/STs.

In this section, we examine the importance of direct changes in education and entry costs relative to the role of growth by allowing for all the costs to potentially change between 1983 and 2012. Specifically, we conduct an alternative quantitative exercise where re-calibrate the sectorial growth rates as well as the entry and education costs in 2012. There are nine parameters involved: three sectorial growth rates, three levels of costs and three relative costs. We calibrate them targeting nine moments in 2012: three sectoral labor productivity growth rates, the three sectoral relative labor gaps, and the three sectoral relative wage gaps.<sup>1</sup> To ease notations, we define the relative costs for the manufacturing sector, service sector, and education as:

$$\psi_m = \frac{\gamma_n^m}{\gamma_s^m}, \quad \psi_h = \frac{\gamma_n^h - \gamma_n^m}{\gamma_s^h - \gamma_s^m}, \quad \psi_e = \frac{\lambda_s}{\lambda_n}$$
(B.36)

Table 14 summarizes the calibrated parameters in 2012 as well as the corresponding parameters in our baseline calibration where the six cost variables are fixed at 1983 levels. The key differences relative to the 1983 baseline parameters are (a) the relative education cost for SC/STs,  $\psi_e$ , is lower in 2012; (b) the relative cost of sectoral entry for non-SC/STs in 2012 is higher in manufacturing and lower in services, relative to their 1983 levels.

Table 15 below shows the key moments generated from the re-calibrated model. Compared to our baseline results where costs are fixed, the major improvement of the fit lies in the labor gap in the manufacturing sector. This is mainly because of the increase of  $\psi_m$ , which now makes non-SC/STs more willing to move from manufacturing to services. As a result, the labor share gap

<sup>&</sup>lt;sup>1</sup>We re-calibrate the sectorial productivity growth rates because when we allow the costs to change, the implied labor productivity growths in the model would be different from our baseline when the costs are fixed.

Table 14: Parameters									
Calibrated variables									
VARIABLE	VAL	JUE	VARIABLE	VAL	UE				
	baseline	2012		baseline	2012				
		Cost Pa	rameters						
$\gamma_s^m$	20.14	6.40	$\gamma^h_s$	299	89.97				
$\lambda_s$	2.53	2.82	$\psi_m$	1.04	1.08				
$\psi_h$	1.33	1.28	$\psi_e$	1.55	1.43				
	Sectorial Productivity Growth								
$A_g$	1.1436	1.2436	$M_g$	2.1421	2.4062				
$H_g$	2.4068	2.5528							

in manufacturing is closer to the data relative to the baseline version.

To assess the relative contributions of growth and caste-specific costs to the caste wage convergence, we proceed in two stages. First, we eliminate the impact of changing costs by holding the six education and entry costs constant at their 1983 levels. Any wage convergence in this case is solely attributable to growth. These results are included in column (1) of Table 16.

Then we scale all the costs by the compound growth factor  $\frac{A_{2012}^{\theta}M_{2012}^{\eta}H_{2012}^{1-\theta-\eta}}{A_{1983}^{\theta}M_{2983}^{\eta}H_{1983}^{1-\theta-\eta}}$ . Since growth impacts caste gaps in the model solely through its *indirect* effect on the caste-specific costs, any changes in caste gaps in this experiment are solely attributable to *direct* changes in education and entry costs during 1983-2012. Furthermore, to examine the role of education and entry cost separately, in column (2), we only change the education cost parameters while keeping entry costs at the 1983 levels. In column (3), we change the entry costs but keep education costs at 1983 levels.

		1983 2012						
VARIABLE	Notation	Data	Model	Data	Model			
		Bas	BASELINE		GETED			
Wage Gap Agriculture	$\Delta w^a$	1.04	1.04	1.08	1.09			
Wage Gap Manufacture	$\Delta w^m$	1.20	1.20	1.14	1.19			
Wage Gap Service	$\Delta w^h$	1.45	1.45	1.33	1.30			
Labor Share Gap Agri	$\Delta s^a$	0.80	0.85	0.79	0.90			
Labor Share Gap Manuf	$\Delta s^m$	1.43	1.43	1.57	1.58			
Labor Share Gap Serv	$\Delta s^h$	1.61	1.60	1.21	1.23			
Labor Prod Growth Agri	$rac{Ey_{11}^a}{Ey_{83}^a}$	-	-	2.07	2.07			
Labor Prod Growth Manuf	$rac{Ey_{11}^m}{Ey_{83}^m}$	-	-	3.40	3.40			
Labor Prod Growth Serv	$\frac{Ey_{11}^h}{Ey_{83}^h}$	-	-	2.70	2.70			
		BASELINE		Non-T	ARGETED			
Mean educ SC/ST	$\bar{q}_s$	1.81	1.75	4.73	3.53			
Mean educ Non-SC/ST	$ar{q}_n$	4.08	3.86	5.78	6.14			
Total wage gap	$\Delta w$	1.45	1.34	1.30	1.278			

Table 15: Data and Model Moments

Notes: The top panel of the table reports the sectoral caste gaps in employment and wages with all gaps being the ratio of Non-SC/ST to SC/ST, and the sectorial labor productivities. The bottom panel reports the data and model generated of selected non-targeted moments.

		~		
VARIABLE	Notation	Growth	Education	Entry
		(1)	(2)	(3)
Wage Gap Agriculture	$\Delta w^a$	1.05	1.04	1.09
Wage Gap Manufacture	$\Delta w^m$	1.23	1.20	1.19
Wage Gap Service	$\Delta w^h$	1.10	1.38	1.43
Labor Share Gap Agri	$\Delta s^a$	0.85	0.88	0.87
Labor Share Gap Manuf	$\Delta s^m$	3.12	1.47	1.26
Labor Share Gap Serv	$\Delta s^h$	1.17	1.24	1.45
Labor Prod Growth Agri	$rac{Ey^{a}_{11}}{Ey^{a}_{83}} \\ Ey^{m}_{11}$	2.46	0.98	1.24
Labor Prod Growth Manuf	$rac{Ey_{11}^m}{Ey_{83}^m}$	4.15	1.93	2.26
Labor Prod Growth Serv	$\frac{Ey_{11}^h}{Ey_{83}^h}$	2.88	2.09	2.17
Mean educ SC/ST	$\bar{q}_s$	4.62	1.42	2.00
Mean educ Non-SC/ST	$\bar{q}_n$	7.51	2.65	4.21
Total wage gap	$\Delta w$	1.20	1.25	1.32
Notes: All sectoral caste ga Non-SC/ST to SC/ST.	ps in emplo	oyment and	wages are the	ratio of

Table 16: Model Moments with Growth or Relative Cost Changes

From Table 16 we see that with only growth, the total wage gap falls from 1.34 to 1.20. This

is similar to our baseline result. The newly calibrated productivity growth rates are slightly higher than those in the baseline, resulting in slightly more convergence. Moreover, productivity growth moves all the caste gaps in the same direction as the data, and creates the convergence in the education gap. The only unsatisfactory result is that the model with only growth creates too much increase of  $\Delta s^m$  and too much shrink of  $\Delta s^h$ .

In column (2), we fix the entry cost at the 1983 levels and eliminate the impact of growth on real costs by scaling the costs by the factor of labor productivity. In particular, the *relative* education cost falls for SCSTs compared to NSTs. Meanwhile, the *absolute* education costs increase for both castes. In this case, the total wage gap falls to 1.26. The fall of relative education costs create relatively easier entry for SCSTs into the manufacturing and service sectors. This lowers the service and total wage gaps and creates convergence in the labor gap of the service sector. However, the high absolute education costs led to counterfactually lower average education levels than in 1983. As a result, it cannot generate labor productivity growth comparable to what is observed in the data.

Finally, when we only change entry costs, the total wage gap changes only marginally. The relative entry cost of entering the manufacturing sector becomes higher and that of entering service is falling for SCST. This helps to shrink the labor gap in manufacturing, which balances out the overshoot of  $\Delta s^m$  and  $\Delta s^h$  when the impact of growth comes in. However, this force cannot create sizable convergence in all wage gaps. It also fails to create sizable labor productivity growth as well as the education gap convergence. In light of these patterns, we think that growth plays a more significant role in creating the wage and education gap movements in line with the data.

## C Misallocations and Productivity

A key aspect of our model is that labor productivity responds to both exogenous and endogenous factors. The endogenous response arises anytime agents change their schooling and sectoral employment decisions in response to exogenous shocks. This re-sorting changes the human capital of workers as well as the sectoral distribution of the human capital, both of which affect the sectoral and aggregate levels of labor productivity. Put differently, productivity affects talent misallocation but misallocation itself affects productivity in the model. How big is this latter effect?

Worker re-sorting in the model occurs due to changing costs of schooling and sectoral employment which also change the talent misallocations and caste gaps. We evaluate the quantitative importance of the decreasing caste misallocation for labor productivity by comparing sectoral labor productivity growth rates under three scenarios: (i) sectoral entry costs are scaled to aggregate growth; (ii) schooling costs are scaled to aggregate growth; and (iii) both entry costs and schooling costs are scaled to growth. In each experiment, we hit the model with the imputed exogenous productivity growth rates in the baseline case.

Table 17 reports the sectoral productivity growths under the three scenarios as well as the numbers in the baseline case. Comparing the column "Scale both" with the last column shows that the overall and exogenous sectoral productivity growth rates become identical when both costs are scaled. In this case, there is no change in misallocations as the relative real costs of schooling and sectoral employment remain unchanged for the two castes. Hence, the difference between the exogenous sectoral productivity growth and the overall sectoral productivity growth in the baseline case (column "Baseline") is due to changing misallocations.

	Table 17: Changing Misallocations and Productivity Growth								
	Scaling costs								
Variable	Data	Baseline	Scale entry	Scale educ	Scale Both	Exogenous Growth			
$\frac{Ey_{11}^a}{Ey_{83}^a}$	2.07	2.07	2.10	1.00	1.14	1.14			
$rac{Ey_{11}^{\widetilde{m}}}{Ey_{83}^m}$	3.40	3.40	3.78	1.67	2.14	2.14			
$\frac{Ey_{11}^a}{Ey_{83}^a} \\ \frac{Ey_{11}^m}{Ey_{83}^m} \\ \frac{Ey_{11}^m}{Ey_{11}^h} \\ \frac{Ey_{83}^h}{Ey_{83}^h}$	2.70	2.70	2.72	1.71	2.41	2.41			

Table 17: Changing Misallocations and Productivity Growth

The numbers in Table 17 imply that declining misallocations due to endogenous education and sectoral sorting account for 45 percent, 37 percent and 11 percent of overall labor productivity growth in Agriculture, Manufacturing and Services, respectively. If one weights these numbers by the sectoral share parameters  $\theta$ ,  $\eta$  and  $1 - \theta - \eta$ , declining talent misallocation accounts for 39 percent of the labor productivity growth in India during 1983-2012.

# D Welfare Costs of Caste Distortions

The model that we have outlined has two sources of differences across castes: the costs of schooling and the costs of entry into sectoral labor markets. How expensive are these distortions? How much would SC/ST welfare rise if these distortions were removed? Would non-SC/STs gain as well? What would be the aggregate welfare gains? In order to interpret the differences across castes in schooling and sectoral entry costs as distortions, we now provide a tax representation of these costs. Specifically, we define:

$$\begin{split} \lambda_s &= \lambda_n + \tau_\lambda \\ \gamma_s^k &= \gamma_n^k + \tau_\gamma^k, \quad k = m,h \end{split}$$

where  $\tau_{\lambda}$  is the tax on schooling and  $\tau_{\gamma}^{k}$ , k = m, h is the tax on sectoral entry costs borne by SC/ST agents. Note that since  $\gamma_{s}^{k} < \gamma_{n}^{k}$ , k = m, h under our calibration in Table 1,  $\tau_{\gamma}^{k} < 0$ , k = m, h, i.e., affirmative action will act as a subsidy for SC/STs in accessing sectoral labor markets.

Using  $T_i$  to denote per capita public expenditure, the government's budget constraint is

$$L\left[s\int_{\underline{a}}^{\bar{a}}T_{i}dG(a_{i})+n\int_{\underline{a}}^{\bar{a}}T_{i}dG(a_{i})\right] = L\left[s\int_{\underline{a}}^{\bar{a}}\tau_{\lambda}q_{i,s}^{*}dG(a_{i})\right] + L\left[s\int_{\hat{a}_{s}^{m}}^{\tilde{a}_{s}^{h}}\tau_{\gamma}^{m}\phi dG(a_{i})+s\int_{\tilde{a}_{s}^{h}}^{\bar{a}}\tau_{\gamma}^{h}\phi dG(a_{i})\right]$$
(D.37)

where  $q_{i,s}^*$  stands for the optimal choices of schooling given by equations 3.7-3.9.

This formulation of the cost differences as tax distortions leaves unchanged the production details of the model since we retain the same calibrated  $\lambda_n, \lambda_n, \gamma_n^k, \gamma_s^k$  as in Table 1. The consumption side of the model however does get affected by this reformulation since taxes could be either rebated to the public or consumed by the government. We shall examine both possibilities below.

To assess the welfare costs of caste distortions, we compare aggregate outcomes under the baseline case with two sets of counterfactual experiments: (a) equal sectoral entry costs for the two castes; and (b) equal schooling and sectoral entry costs. We conduct this comparison both with and without tax rebates. Note that since the two castes draw their ability endowments from the same distribution, equalizing both caste distortions would eliminate all caste gaps.

Table 18 reports the results for the case when taxes are not rebated. The last column of the Table ("all equal") in the left panel (1983) shows that equalizing all costs equalizes average consumption for both castes since they both draw from the same ability distribution. This translates into an increase in average consumption for SC/STs by 58.8 percent in 1983 and 53.9 percent in 2012. Interestingly, it also marginally raises the average consumption of non-SC/STs in both years. This occurs due to the rise in aggregate output that is induced by the removal of caste distortions.

Aggregate output,  $Y_f$ , rises by 11.4 percent in 1983. This is the static gain from removing caste distortions. The corresponding output gain in 2012 is 8.4 percent. The increase in average per

#### HNATKOVSKA-HOU-LAHIRI: CASTE CONVERGENCE

	Table 10. Wehate Costs of Caste Distortions Chief no repate								
		1983	2012						
Variable	Baseline	$\gamma$ 's equal	all equal	Baseline	$\gamma$ 's equal	all equal			
$C_s$	101.29	98.22	160.1	226.78	223.29	349.0			
$C_n$	160.00	160.27	160.1	346.45	349.02	349.0			
C	145.32	144.76	160.1	316.53	317.59	349.0			
$Y_a$	134.04	133.72	146.3	287.97	288.91	310.6			
$Y_m$	220.68	224.42	241.1	485.35	479.88	515.3			
$Y_h$	293.97	288.55	325.6	1025.8	1035.57	1127.0			
$Y_f$	195.87	194.73	218.13	510.71	512.50	553.6			

Table 18: Welfare Costs of Caste Distortions Under No Rebate

Notes: The table reports average consumption of each caste as well as per capita outputs of the sectoral and final goods under various parameter configurations for schooling and sectoral entry costs when taxes are not rebated to the public.

capita consumption, C, from removing all caste distortions in this economy is 10.2 percent in 1983 and 10.3 percent in 2012.

How do these estimates change when the caste taxes are rebated back to the public in the form of lump-sum transfers? Table 19 reports the results for average consumption in this case. Since the production side of the economy is unaffected by whether taxes are rebated or not, the output numbers in this case are identical to those in Table 18 above.

		1983			2012	
Variable	Baseline	$\gamma$ 's equal	all equal	Baseline	$\gamma$ 's equal	all equal
$C_s$	110.94	107.48	160.1	250.33	245.39	349.0
$C_n$	169.65	169.53	160.1	370.67	371.12	349.0
C	154.97	154.01	160.1	340.58	339.69	349.0

Table 19: Welfare Costs of Caste Distortions Under Lump-Sum Rebates

Notes: The table reports average consumption of each caste as well as per capita outputs of the sectoral and final goods under various parameter configurations for schooling and sectoral entry costs when taxes are fully rebated to the public.

As one might expect, the tax rebate raises the average consumption of both castes in the distorted baseline economy relative to the no-rebate case. Outcomes when all distortions are removed however remain identical to those in Table 18. Consequently, the welfare gains for SC/STs from removing all distortions are now smaller in both years. The average per capita consumption gains for SC/STs is 44.3 percent in 1983 and 39.4 percent in 2012.

The interesting feature of the full rebate case is that removal of all distortions now does hurt

non-SC/STs. Since non-SC/STs receive net positive transfers from SC/STs through the tax rebates under the distorted economy, the removal of all taxes reduces their net income. This effect is strong enough for removal of distortions to cause a reduction in the average consumption of non-SC/STs.

The main takeaway from these results is that there are significant welfare gains from removing caste distortions. These gains are very high for SC/STs. Strikingly, in the realistic case of no tax rebates, reforms that remove all caste distortions also raise the welfare of non-SC/STs indicating that the reforms are Pareto improvements.